

Machine Learning Schemes

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1

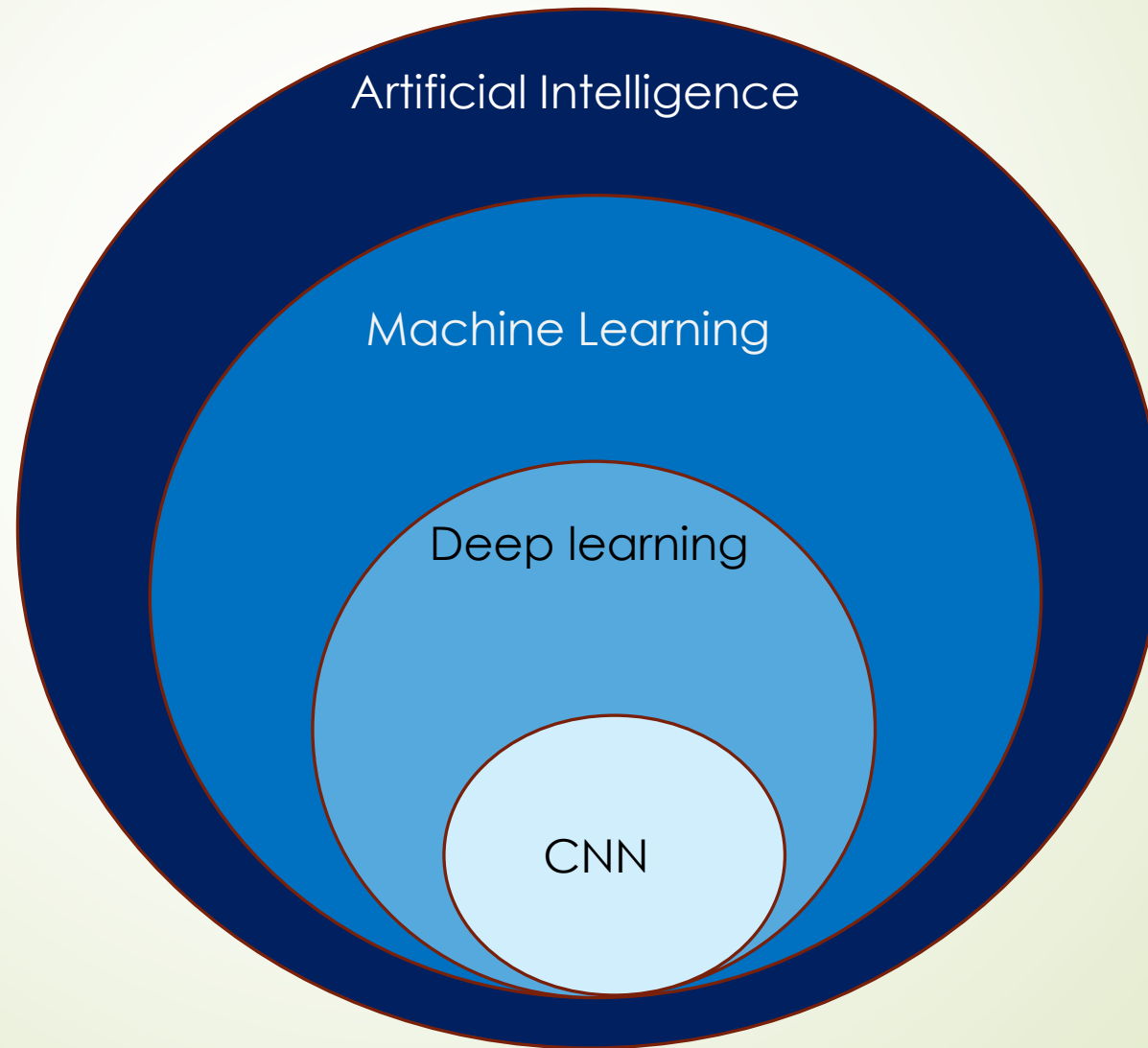
Artificial intelligence in applications. Modeling, Machine Learning and Data Classifier Performance

9:45 am - 11:15 am

10-04-2024

AI, ML

2



Machine Learning (Herbert Simon)

Learning is any process by which a system improves performance from experience.

Traditional Programming



Machine Learning



Machine learning Algorithm

Machine Learning is an application of artificial intelligence where a computer/machine learns from the past experiences (input data) and makes future predictions. The performance of such a system should be at least human level.

Diverse Data Types

Prediction

Decision Making

**Learning from
Data**

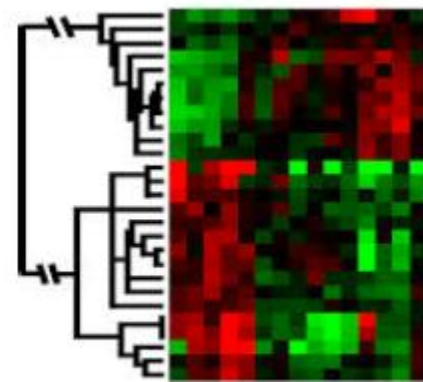
Practical use of ML:

Where can we find ML used?

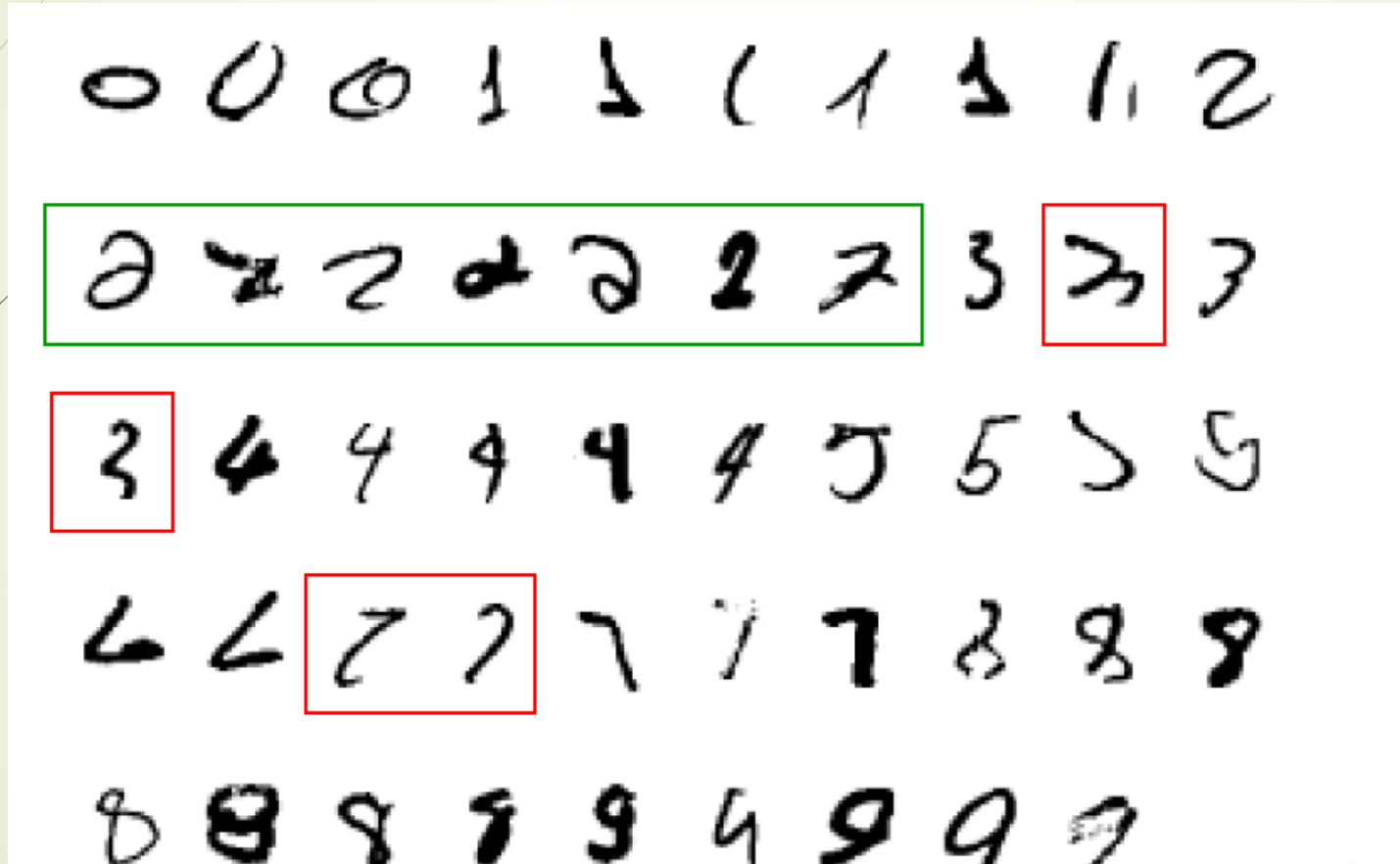
- Self driving cars (Tesla)
- Voice interfaces (Alexa, Siri)
- Face recognition (Google Photos)
- Recomender systems (Netflix, Amazon)
- Games (AlphaGo)
- Character recognition (Post offices)
- Banking systems
- Medical diagnosis
- ML for Human-Computer Interaction

When Do We Use Machine Learning?

- ML is used when:
 - Human expertise does not exist (navigating on Mars)
 - Humans can't explain their expertise (speech recognition)
 - Models must be customized (personalized medicine)
 - Models are based on huge amounts of data (genomics)



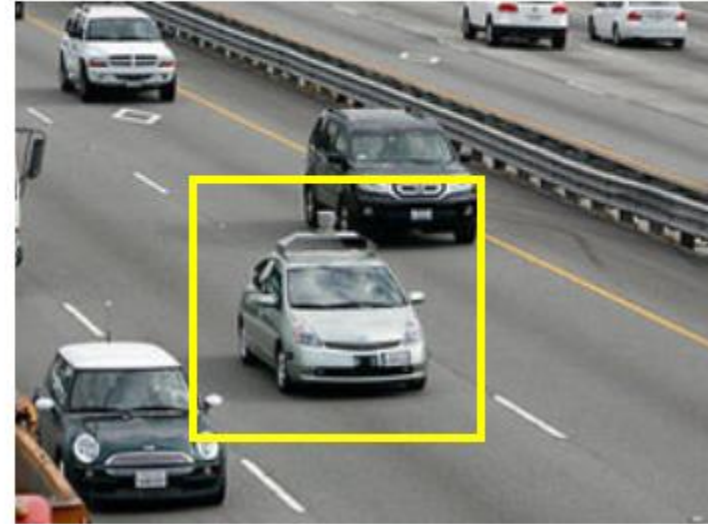
A classic example of a task that requires machine learning:
It is very hard to say what makes a 2



Some more examples of tasks that are best solved by using a learning algorithm

- Recognizing patterns:
 - Facial identities or facial expressions
 - Handwritten or spoken words
 - Medical images
- Generating patterns:
 - Generating images or motion sequences
- Recognizing anomalies:
 - Unusual credit card transactions
 - Unusual patterns of sensor readings in a nuclear power plant
- Prediction:
 - Future stock prices or currency exchange rates
- Slide credit: Geoffrey Hinton
- Web search
- Computational biology
- Finance
- E-commerce
- Space exploration
- Robotics
- Information extraction
- Social networks
- Debugging software

Autonomous Cars

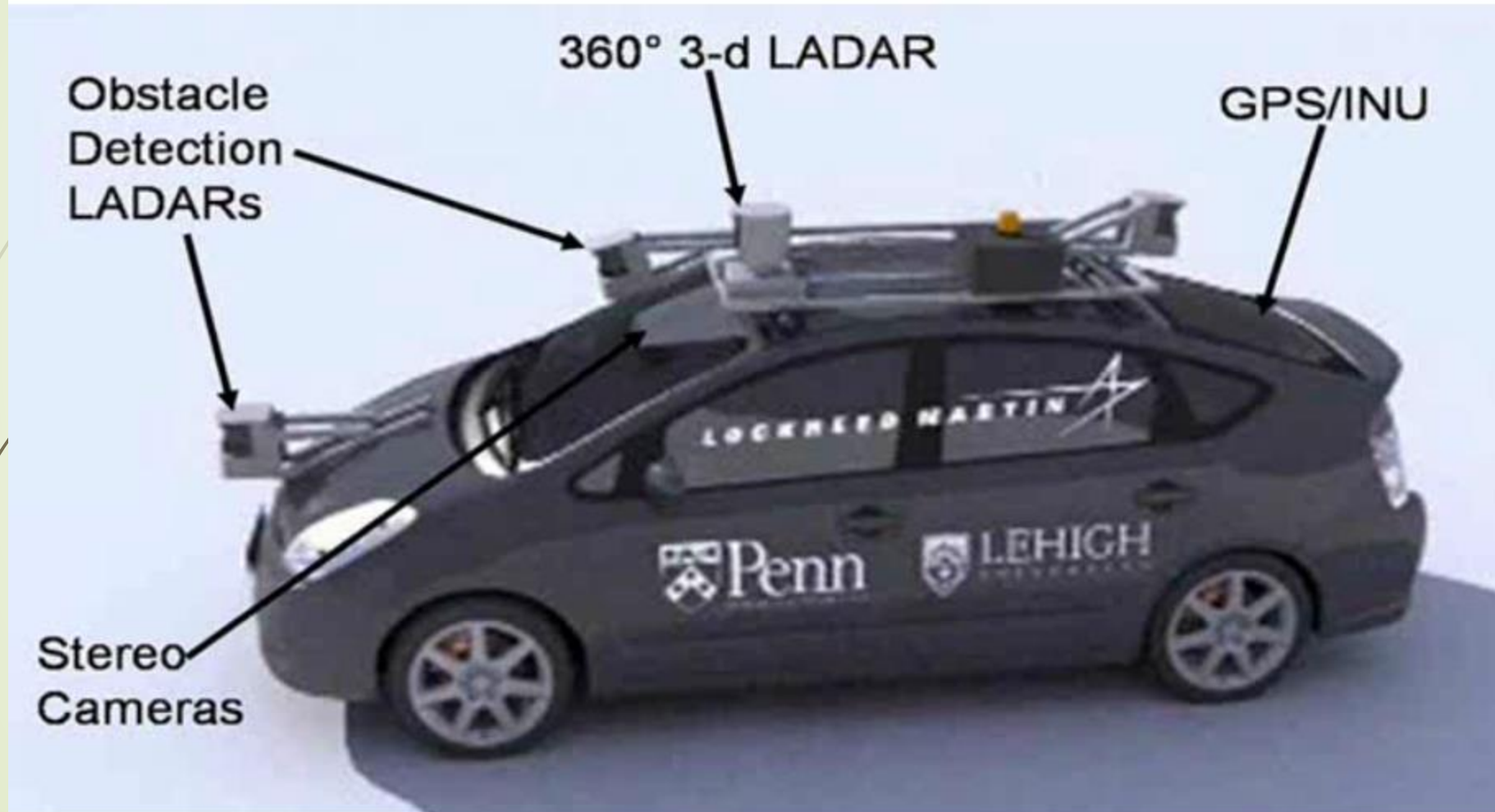


- Nevada made it legal for autonomous cars to drive on roads in June 2011
- As of 2013, four states (Nevada, Florida, California, and Michigan) have legalized autonomous cars

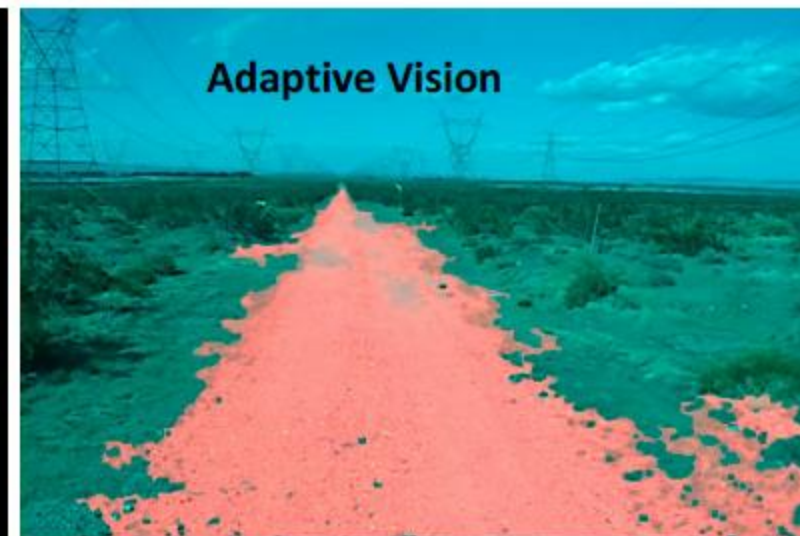
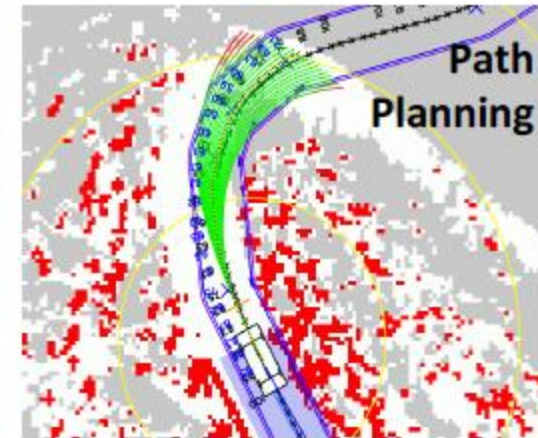
Penn's Autonomous Car →



Autonomous Car Sensors



Autonomous Car Technology

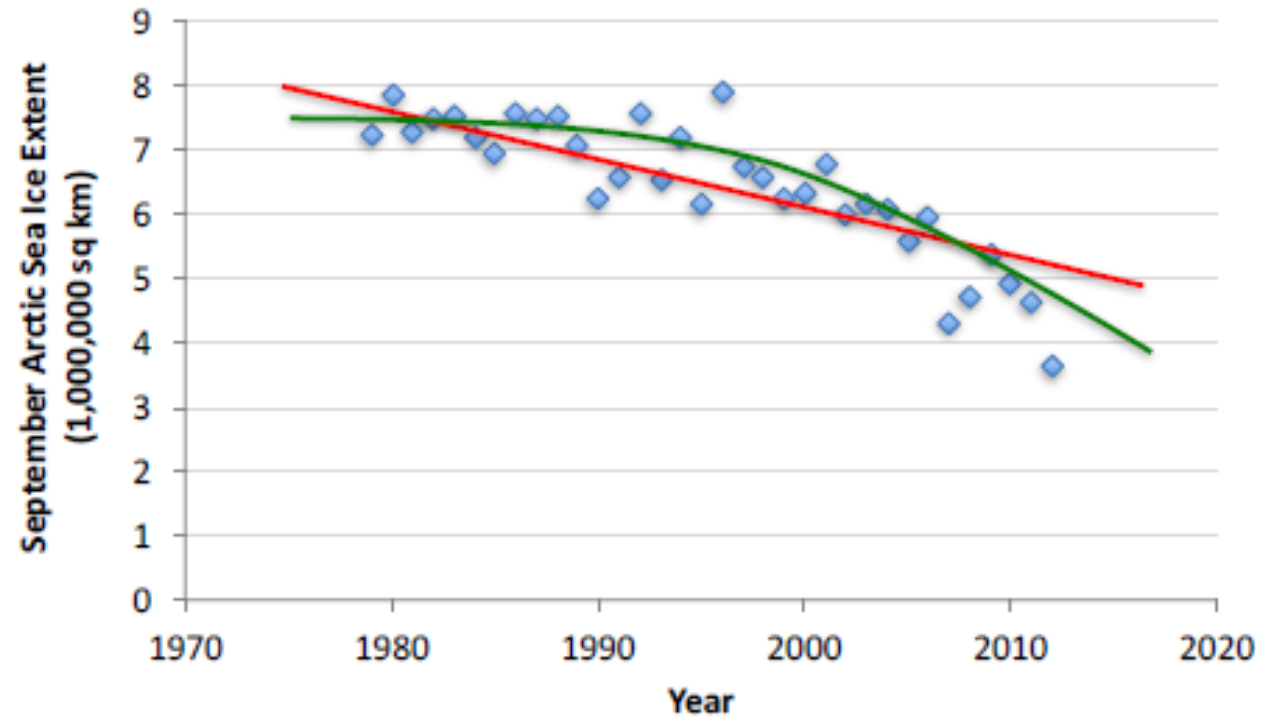


Types of Learning

- **Supervised (inductive) learning**
 - Given: training data + desired outputs (labels)
- **Unsupervised learning**
 - Given: training data (without desired outputs)
- **Semi-supervised learning**
 - Given: training data + a few desired outputs
- **Reinforcement learning**
 - Rewards from sequence of actions

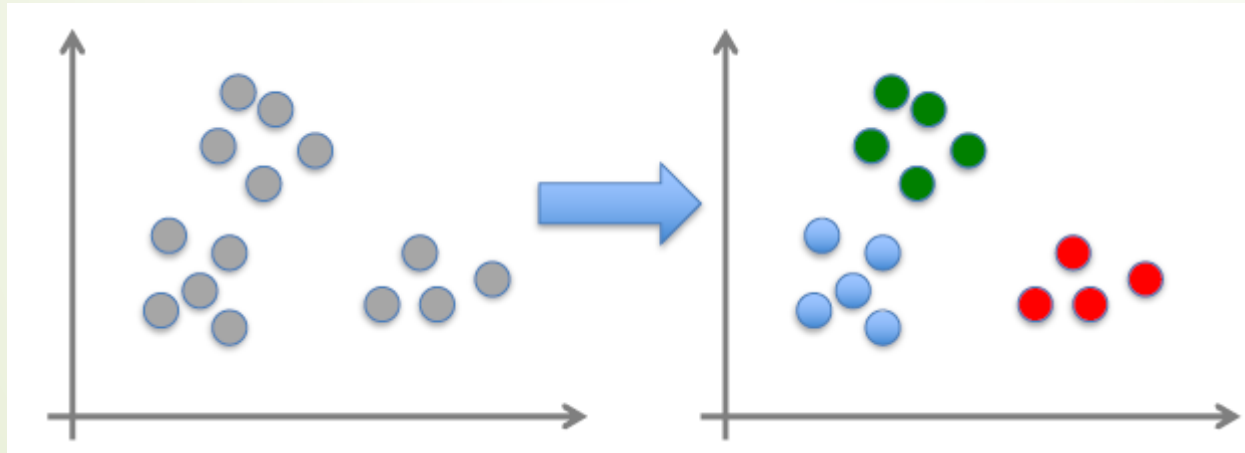
Supervised Learning: Regression

- Given $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$
- Learn a function $f(x)$ to predict y given x
 - y is real-valued == regression



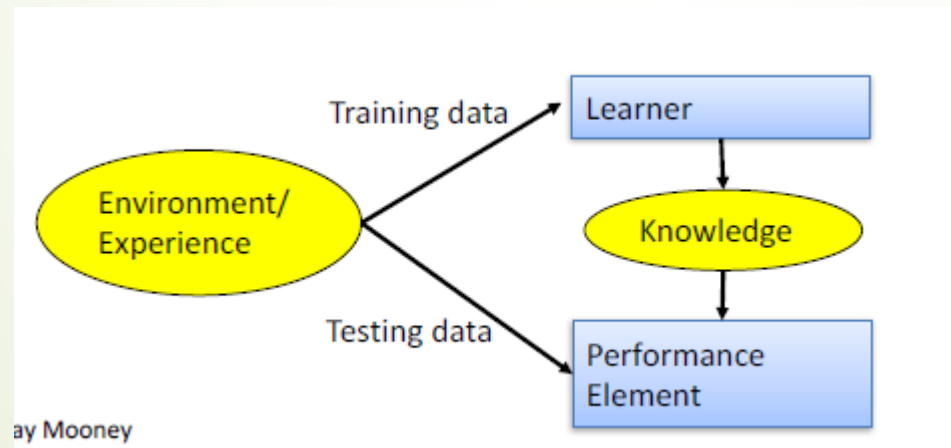
Unsupervised Learning

- Given x_1, x_2, \dots, x_n (without labels)
- Output hidden structure
 - E.g., clustering



Designing a Learning System

- Choose the training experience
- Choose exactly what is to be learned
 - i.e. the **target function**
- Choose how to represent the target function
- Choose a learning algorithm to infer the target function from the experience



Every ML algorithm has three components:

- – Representation
- – Optimization
- – Evaluation

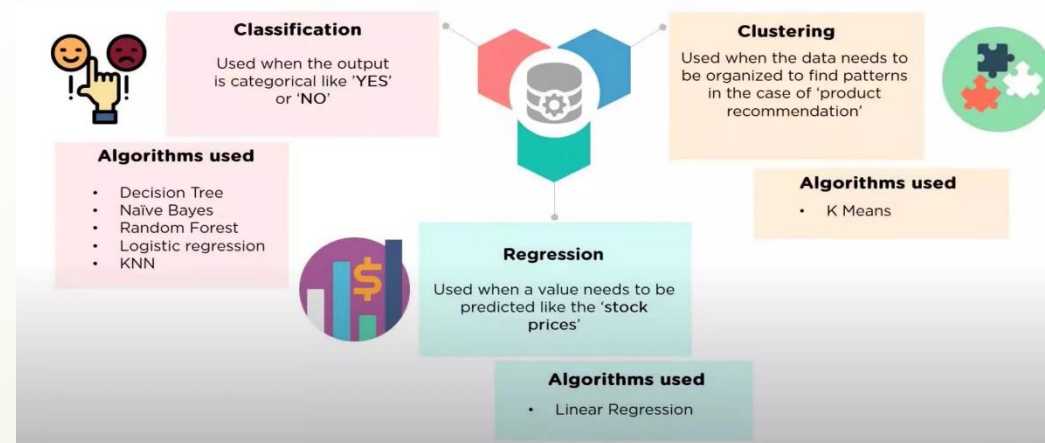
Various Function Representations

- Numerical functions
 - Linear regression
 - Neural networks
 - Support vector machines
- Symbolic functions
 - Decision trees
 - Rules in propositional logic
 - Rules in first-order predicate logic
 - Instance-based functions
 - Nearest-neighbor
- Probabilistic Graphical Models
 - Naïve Bayes
 - Bayesian networks
 - Hidden-Markov Models (HMMs)
 - Markov network

Machine Learning Algorithm



Types In Machine Learning



Evaluation

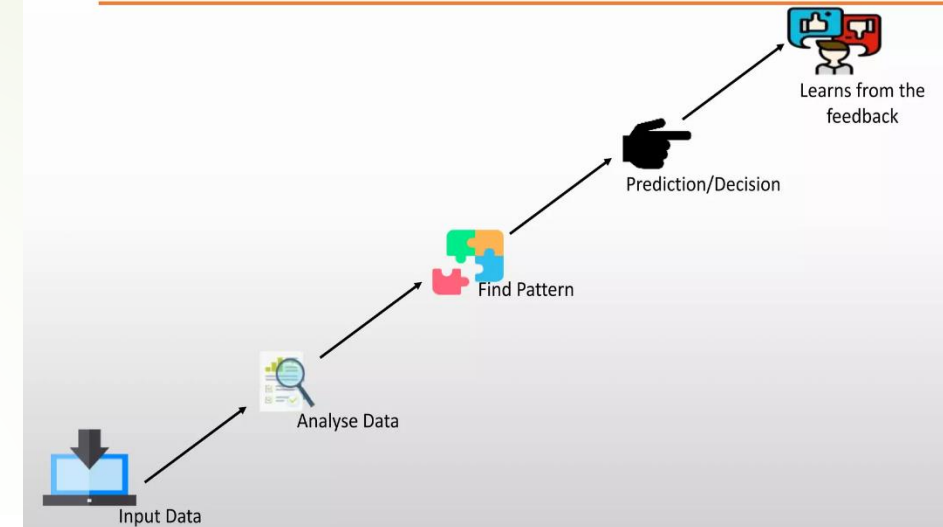
- Accuracy
- Precision and recall
- Squared error
- Likelihood
- Posterior probability
- Cost / Utility
- Margin
- Entropy

- etc.

Types In Machine Learning

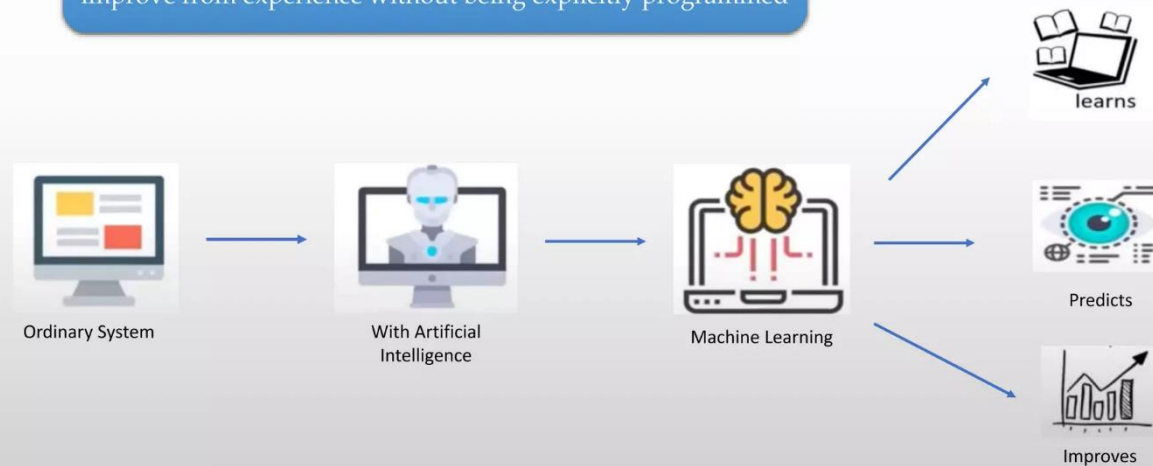


Machine Learning Process



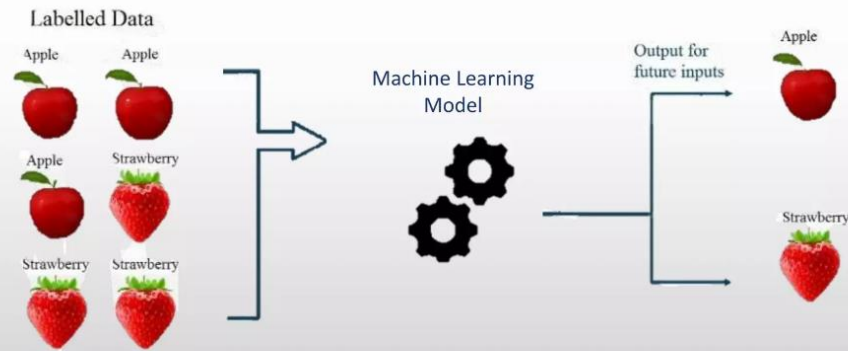
What is Machine Learning?

Machine Learning is an application of Artificial Intelligence (AI) that provides system the ability to automatically learn and improve from experience without being explicitly programmed



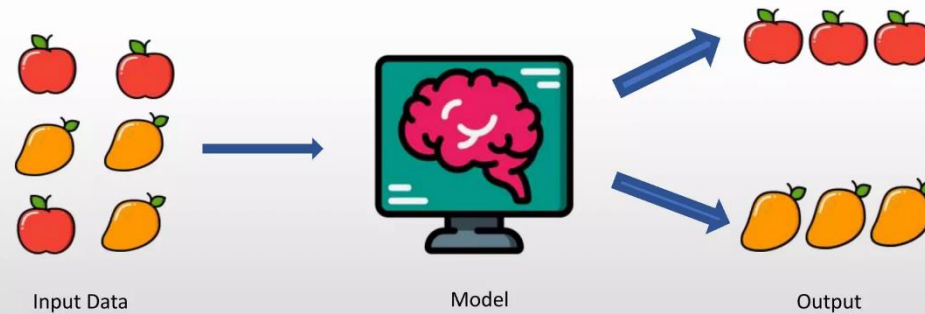
Types In Machine Learning

1. Supervised Machine Learning



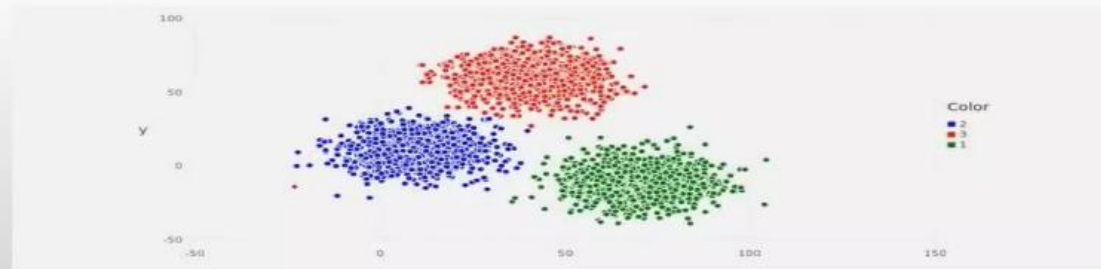
Types In Machine Learning

2. Unsupervised Machine Learning

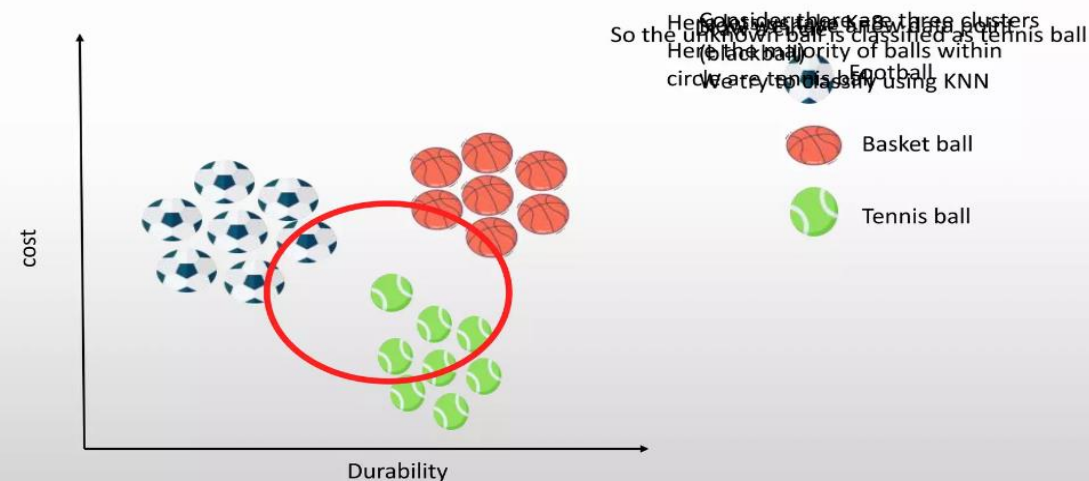


K-Nearest neighbours

- K Nearest Neighbour is a simple algorithm that stores all the available cases and classifies the new data or case based on a similarity measure. It is mostly used to classifies a data point based on how its neighbours are classified.
- In K Nearest neighbour K can be a integer greater than 1. So ,for every new data point we want to classify, we compute to which neighbouring group it is closest.



K-Nearest neighbours Example



Linear Regression

- Linear regression attempts to model the relationship between two variables by fitting a linear equation to observed data. One variable is considered to be an explanatory variable, and the other is considered to be a dependent variable. For example, a modeler might want to relate the weights of individuals to their heights using a linear regression model.

Histogram

Import libraries

I imported several libraries for the project: numpy: To work with arrays pandas: To work with csv files and dataframes matplotlib: To create charts use define parameters using rcParams and color them with cm.rainbow warnings: To ignore all warnings which might be showing up in the notebook due to past/future depreciation of a feature train_test_split: To split the dataset into training and testing data StandardScaler: To scale all the features, so the Machine Learning model better adapts to the dataset Next, I imported all the necessary Machine Learning

```
In [1]: # Basic
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from matplotlib import rcParams
from matplotlib.cm import rainbow
%matplotlib inline
import warnings
warnings.filterwarnings('ignore')

# Other Libraries
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler

# Machine Learning
from sklearn.neighbors import KNeighborsClassifier
from sklearn.svm import SVC
from sklearn.tree import DecisionTreeClassifier
from sklearn.ensemble import RandomForestClassifier
```

Import dataset

After downloading the dataset from Kaggle, I saved it to my working directory with the name dataset.csv. Next, I used read_csv() to read the dataset and store it to the dataset variable. Before any analysis, I just wanted to take a look at the data. So, I used the info() method.

```
In [4]: df=pd.read_csv('heart.csv')
```

```
In [5]: df.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 303 entries, 0 to 302
Data columns (total 14 columns):
 #   Column      Non-Null Count  Dtype  
---  -
 0   age         303 non-null   int64  
 1   sex         303 non-null   int64  
 2   cp          303 non-null   int64  
 3   trestbps    303 non-null   int64  
 4   chol        303 non-null   int64  
 5   fbs         303 non-null   int64  
 6   restecg     303 non-null   int64  
 7   thalach     303 non-null   int64  
 8   exang       303 non-null   int64
```


Data Processing

To work with categorical variables, we should break each categorical column into dummy columns with 1s and 0s. Let's say we have a column Gender, with values 1 for Male and 0 for Female. It needs to be converted into two columns with the value 1 where the column would be true and 0 where it will be false. Take a look at the Gist below.

To get this done, we use the `get_dummies`

To get this done, we use the `get_dummies()` method from pandas. Next, we need to scale the dataset for which we will use the `StandardScaler`. The `fit_transform()` method of the scaler scales the data and we update the columns.

```
In [16]: df = pd.get_dummies(df, columns = ['sex', 'cp', 'fbs', 'restecg', 'exang', 'slope', 'ca', 'thal'])
standardScaler = StandardScaler()
columns_to_scale = ['age', 'trestbps', 'chol', 'thalach', 'oldpeak']
df[columns_to_scale] = standardScaler.fit_transform(df[columns_to_scale])
```

The dataset is now ready. We can begin with training our models.

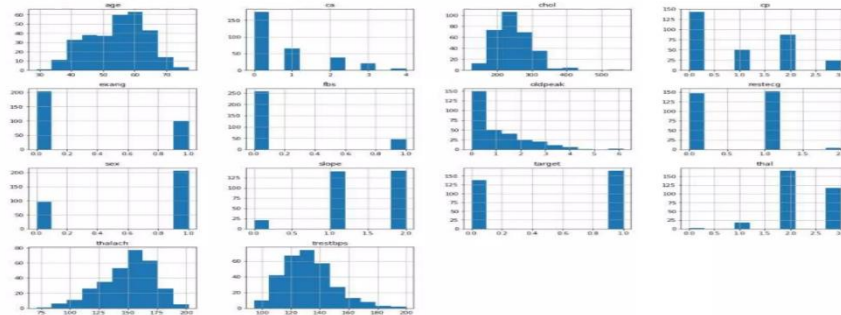
Machine Learning In this project, I took 4 algorithms and varied their various parameters and compared the final models. I split the dataset into 67% training data and 33% testing data.

```
In [18]: y = df['target']
X = df.drop(['target'], axis = 1)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size = 0.33, random_state = 0)
```

Histogram

The best part about this type of plot is that it just takes a single command to draw the plots and it provides so much information in return. Just use `dataset.hist()`.

```
In [12]: df.hist()
Out[12]: array([[<matplotlib.axes._subplots.AxesSubplot object at 0x000001C76874DEC8>,
<matplotlib.axes._subplots.AxesSubplot object at 0x000001C76874DEC8>,
<matplotlib.axes._subplots.AxesSubplot object at 0x000001C76874DEC8>,
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<matplotlib.axes._subplots.AxesSubplot object at 0x000001C76874DEC8>],
dtype=object)
```



Bar Plot for Target Class

It's really essential that the dataset we are working on should be approximately balanced. An extremely imbalanced dataset can render the whole model training useless and thus, will be of no use.

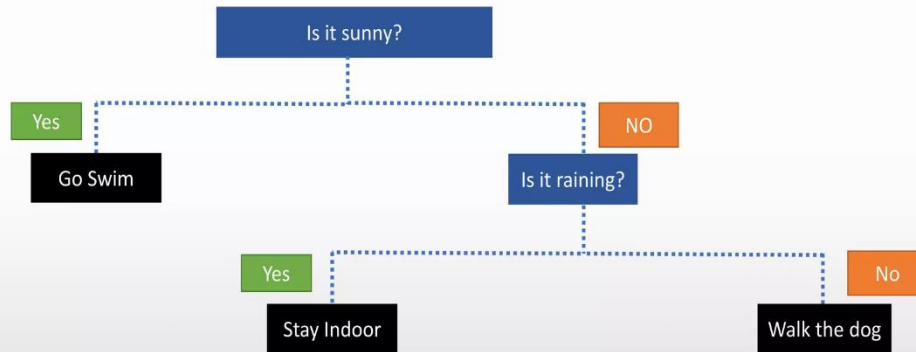
Let's say we have a dataset of 100 people with 99 non-patients and 1 patient. Without even training and learning anything, the model can always say that any new person would be a non-patient and have an accuracy of 99%. However, as we are more interested in identifying the 1 person who is a patient, we need balanced datasets so that our model actually learns.

```
In [14]: rcParams['figure.figsize'] = 8, 6
plt.bar(df['target'].unique(), df['target'].value_counts(), color = ['red', 'green'])
plt.xticks([0, 1])
plt.xlabel('Target Classes')
plt.ylabel('Count')
plt.title('Count of each Target Class')
```

```
Out[14]: Text(0.5, 1.0, 'Count of each Target Class')
```



Decision Tree Example

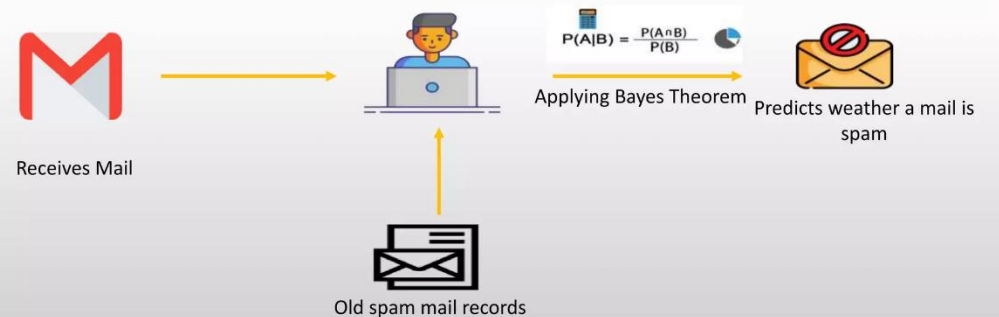


Decision Tree

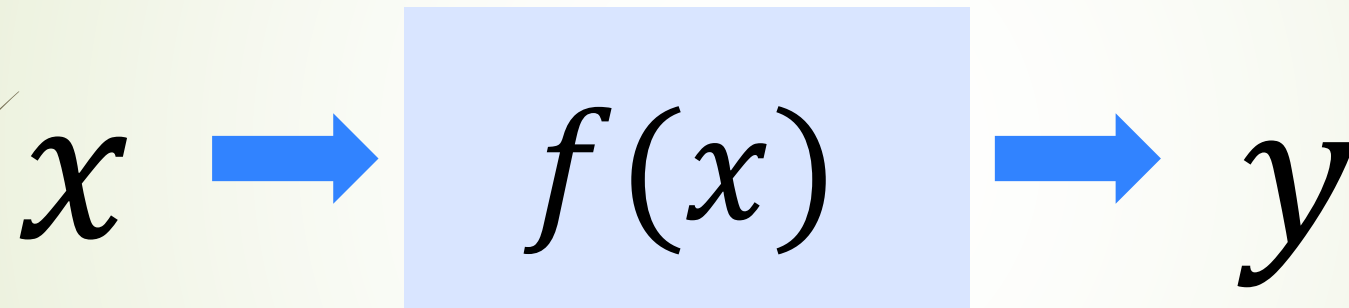
Decision Tree : Decision tree is the most powerful and popular tool for classification and prediction. A Decision tree is a flowchart like tree structure, where each internal node denotes a test on an attribute, each branch represents an outcome of the test, and each leaf node (terminal node) holds a class label.

Naive Bayes

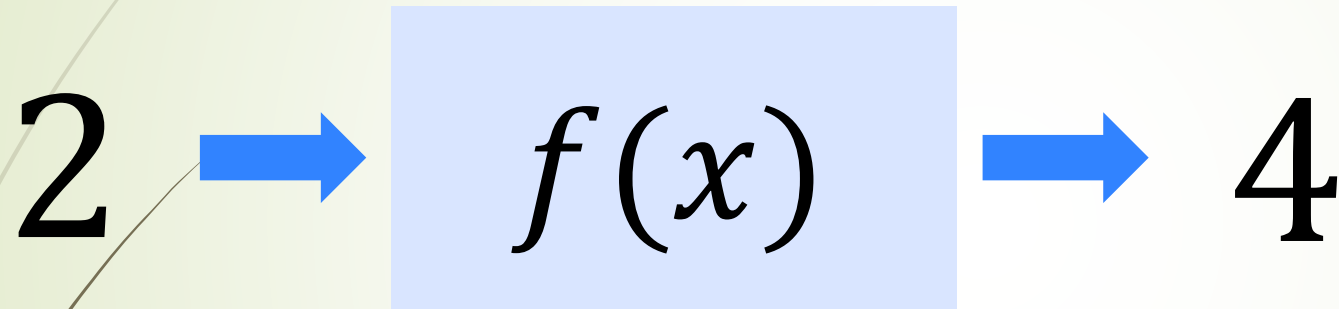
The Naive Bayes Classifier technique is based on conditional probability and is practically suited when the complexity of inputs is high



Machine Learning



Machine Learning



Machine Learning

A diagram illustrating a function $f(x) = 2x$. The input value 2 is shown on the left, followed by a blue arrow pointing to a light blue rectangular box containing the function definition $f(x) = 2x$. Another blue arrow points from the box to the output value 4 on the right.

$$2 \rightarrow f(x) = 2x \rightarrow 4$$

Machine Learning

2



$$f(x) = 2x$$



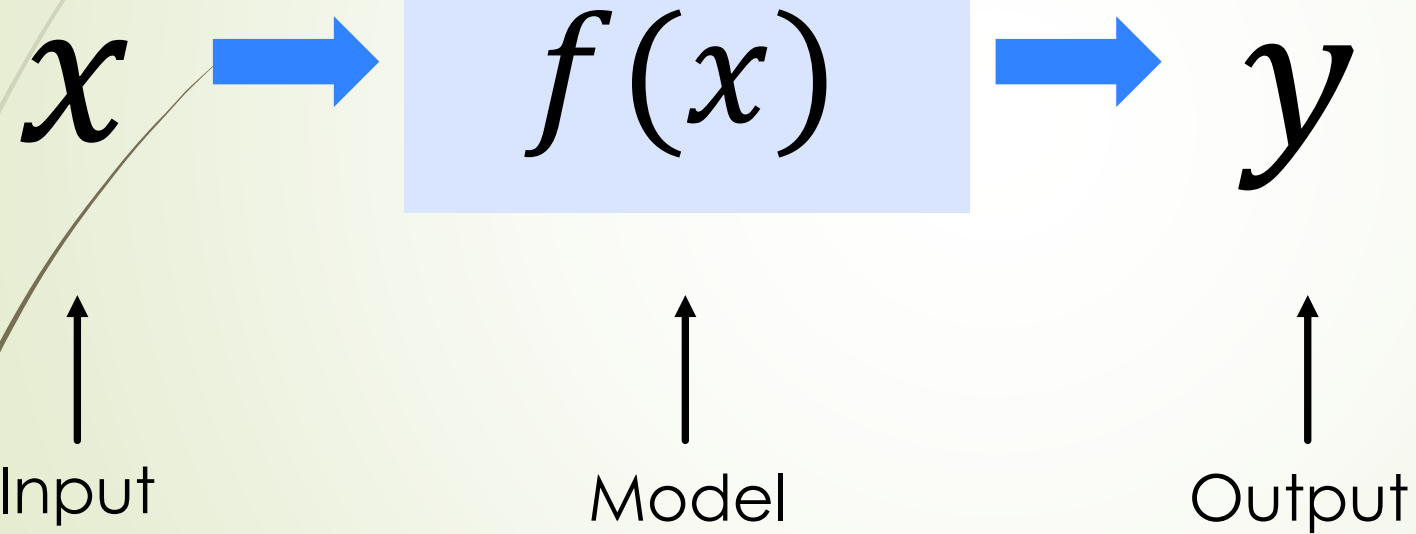
4

↑
Input

↑
Model

↑
Output

Machine Learning



Machine Learning

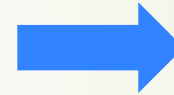
32



x



$f(x)$



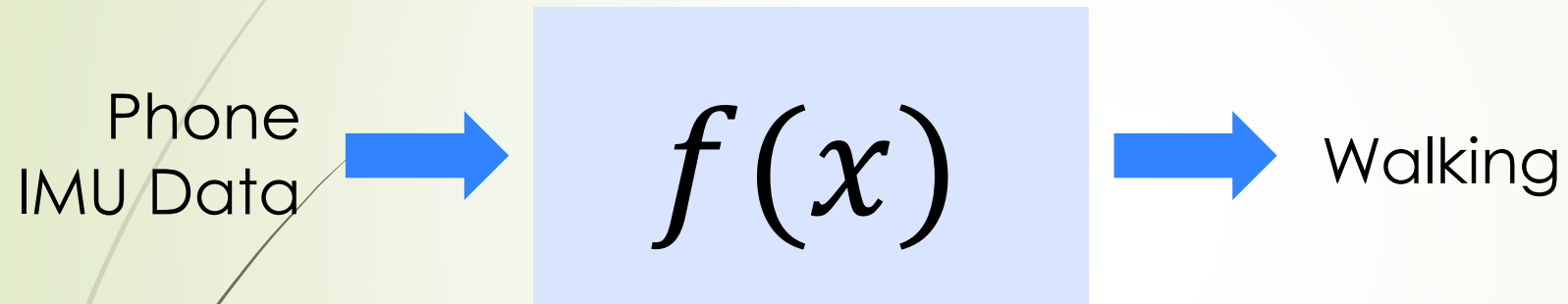
Walking



Model?

*human activity recognition

33 Introduction into Machine Learning



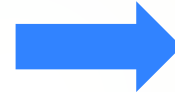
↑
Model?

*human activity recognition

Machine Learning



$f(x)$



dog



Model?

*object recognition

Machine Learning



$$f(x)$$



speaker



Model?

*object recognition

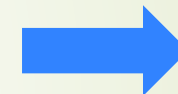
Machine Learning



Phone
IMU Data



$f(x)$



30 years



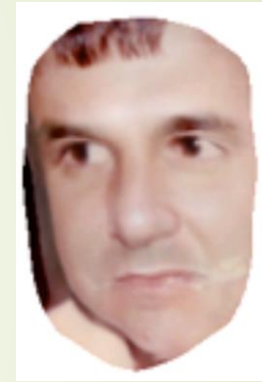
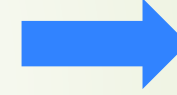
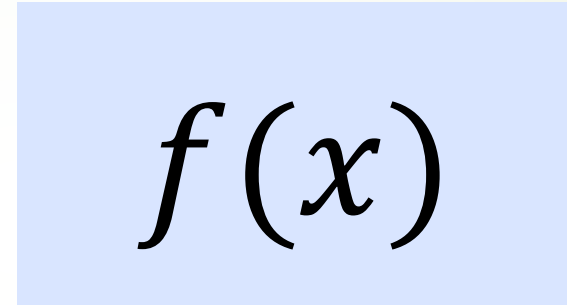
Model?

Gil Levi, and Tal Hassner. "Age and gender classification using convolutional neural networks." In Proceedings of the CVPR workshops. 2015. IEEE: <https://doi.org/10.1109/CVPRW.2015.7301352>

Machine Learning



Phone
IMU Data



Model?

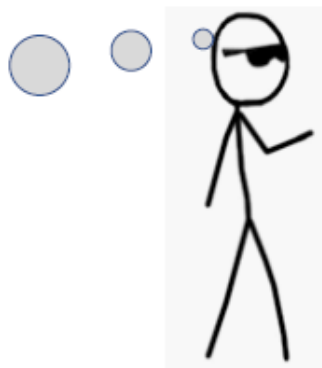
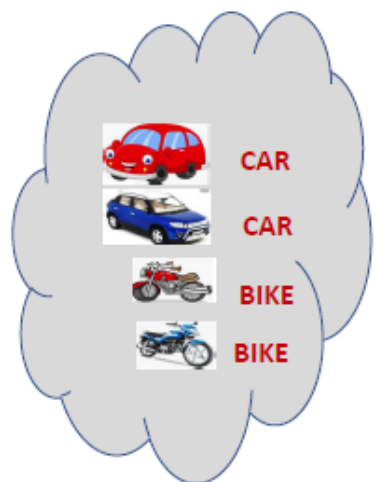
Ira Kemelmacher-Shlizerman, Supasorn Suwajanakorn, and Steven M. Seitz. 2014. Illumination-aware age progression. In Proceedings of the CVPR 2014. IEEE. DOI: <https://doi.org/10.1109/CVPR.2014.426>



Human can learn from past experience
and make decision of its own



What is this object?



It is a CAR

Let us ask the same question to him

39



What is this object?



[But, he is a human being. He can observe and learn]

40

Let us make him learn



show him



CAR



CAR



BIKE



BIKE

Let us ask the same question now

What is this object?



CAR



CAR



BIKE



BIKE

Past experience

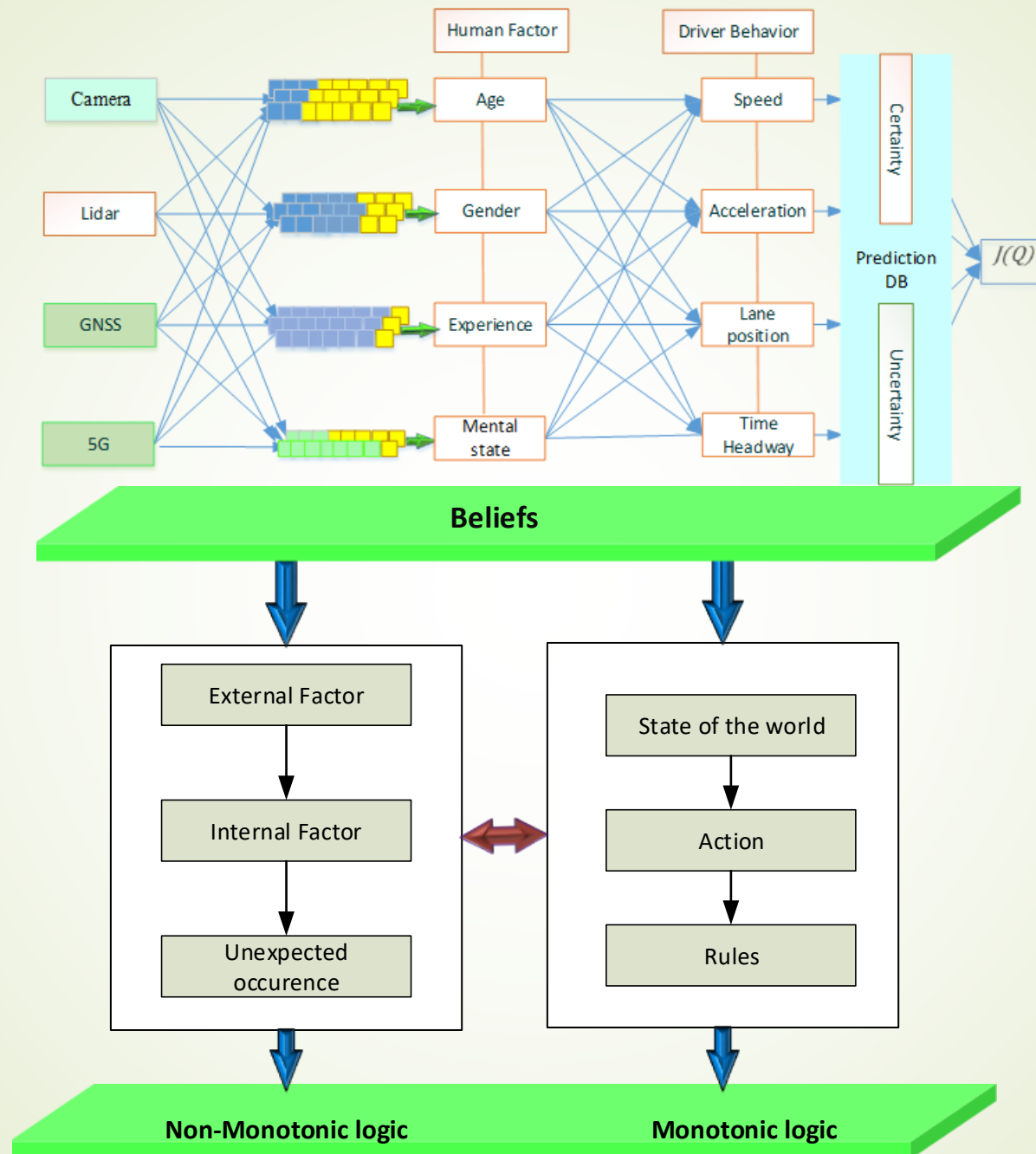
Let us ask the same question now



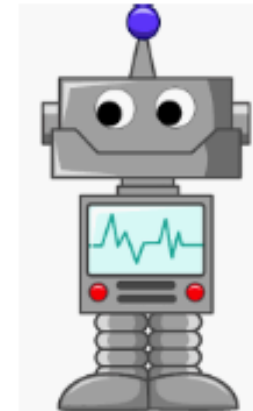
What is this object?







What about a Machine ?



Machines follow instructions

[It can not take decision of its own]

We can ask a machine

- To perform an arithmetic operations such as
 - Addition
 - Multiplication
 - Division

- Comparison
- Print
- Plotting a chart

[We want a machine to act like a human]



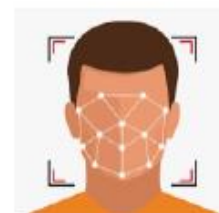
Price in 2025?

[predict the price in future]



I ~~made~~ met him yesterday

[Natural Language understand, and correct grammar]



recognize face

[Recognize Faces]

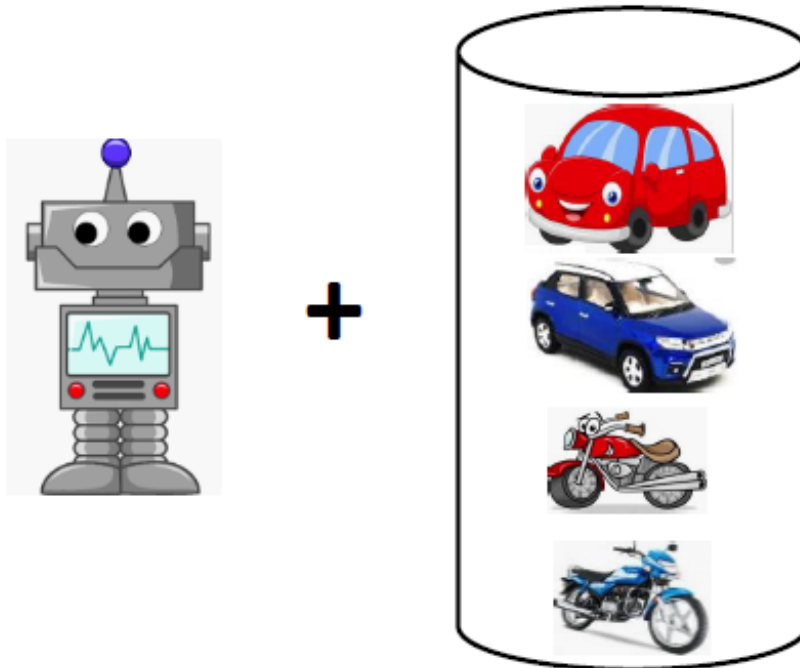


[What do we do?

Just like, what we did to human,

we need to provide experience
to the machine.

]

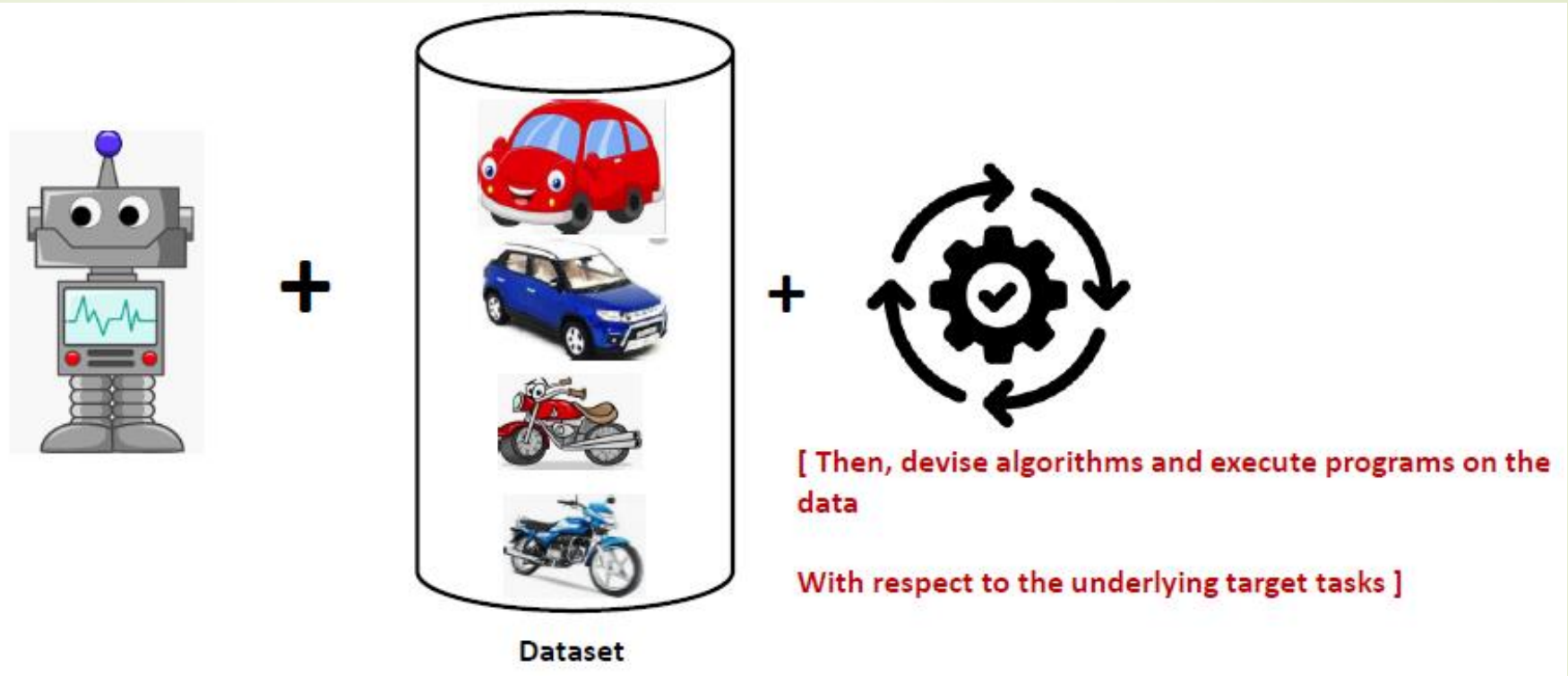


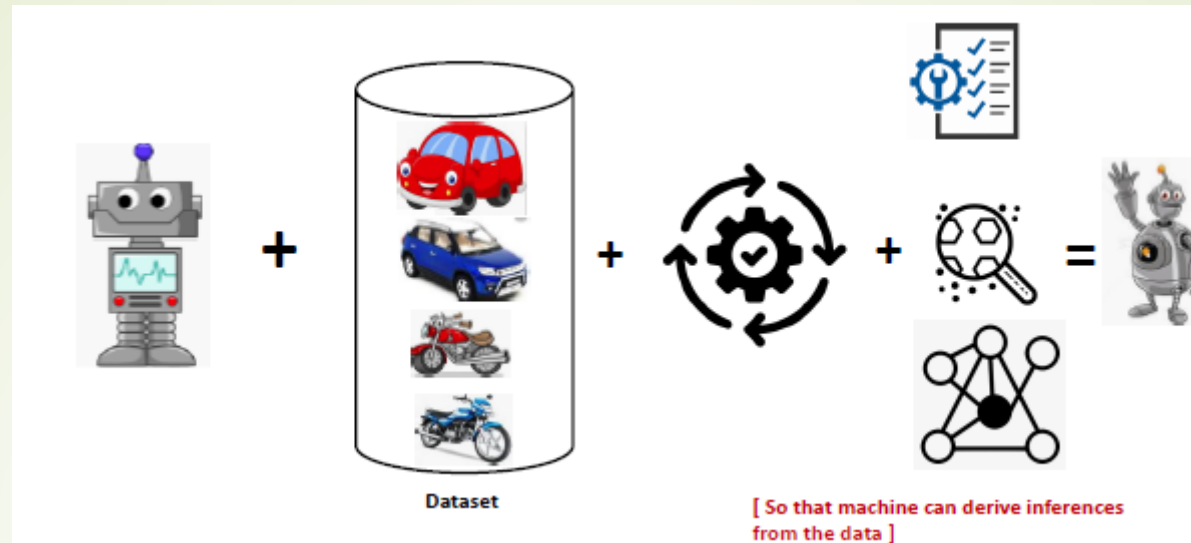
Dataset

[
This what we called as Data
or Training dataset

So, we first need to provide
training dataset to the
machine

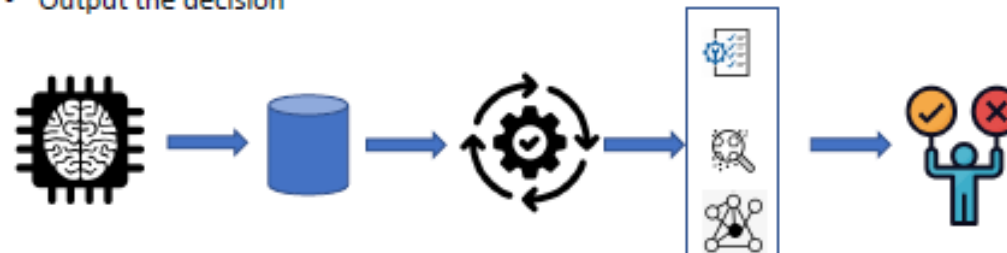
]



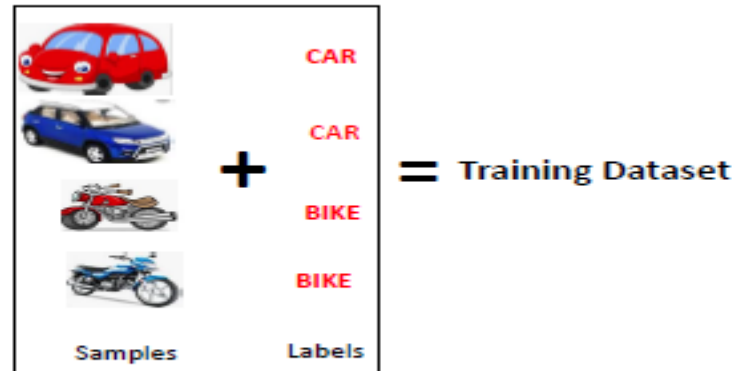


Given a machine learning problem

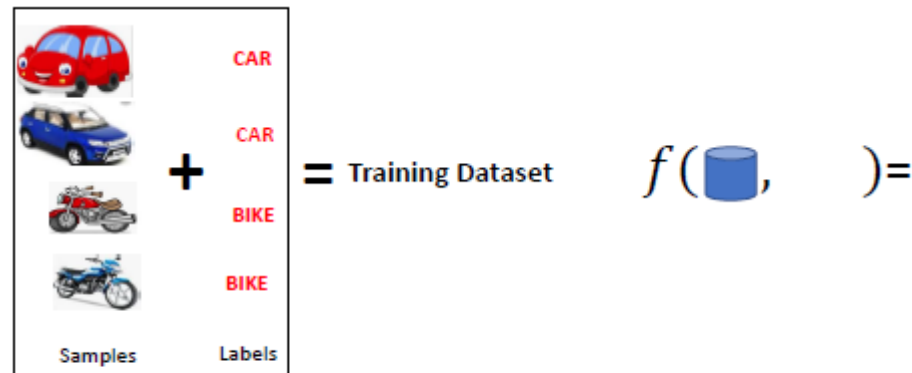
- Identify and create the appropriate dataset
- Perform computation to learn
 - Required rules, pattern and relations
- Output the decision



What is Supervised Learning?



[In supervised learning, we need some thing called a Labelled Training Dataset]



[Given a labelled dataset, the task is to devise a function which takes the dataset, and a new sample, and produces an output value.]

	CAR
	CAR
	BIKE
	BIKE
Samples	Labels

+

= Training Dataset

$$f(\text{dataset}, \text{new sample}) =$$

[Given a labelled dataset, the task is to devise a function which takes the dataset, and a new sample, and produces an output value.]

31

	CAR
	CAR
	BIKE
	BIKE
Samples	Labels

+

= Training Dataset

Classification

$$f(\text{dataset}, \text{new sample}) = \text{CAR}$$

[If the possible output values of the function are predefined and discrete/categorical, it is called Classification

	CAR
	CAR
	BIKE
	BIKE
Samples	Labels

+

= Training Dataset

$$f(\text{dataset}, \text{new sample}) = \text{CAR}$$

[Given a labelled dataset, the task is to devise a function which takes the dataset, and a new sample, and produces an output value.]



+

= Training Dataset

Classification

$$f(\text{bus icon}, \text{bus icon}) = \text{CAR}$$

[Predefined classes means, it will produce output only from the labels defined in the dataset. For example even if we input a bus, it will produce either CAR or BIKE]

34



Elephant



Tiger

Dataset



Elephant

Classifier



Identify the Animal ?

Regression



Dataset

Regression

$$f(\text{house icon}) = 20500.50$$

[If the possible output values of the function are continuous real values, then it is called Regression

The classification and Regression problems are supervised, because the decision depends on the characteristics of the ground truth labels or values present in the dataset, which we define as experience

What is Unsupervised Learning



~~CAR~~



~~CAR~~



~~BIKE~~



~~BIKE~~

Dataset

[In the unsupervised learning, we do not need to know the labels or Ground truth values]



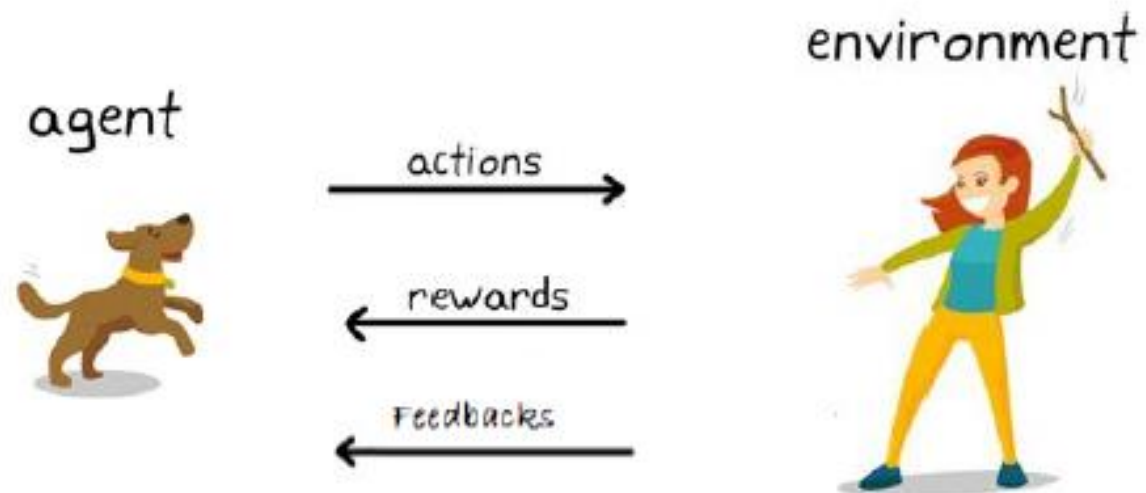
Dataset



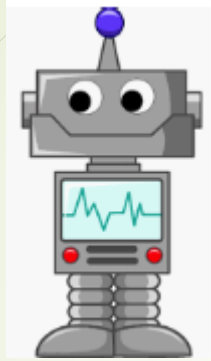
Clustering

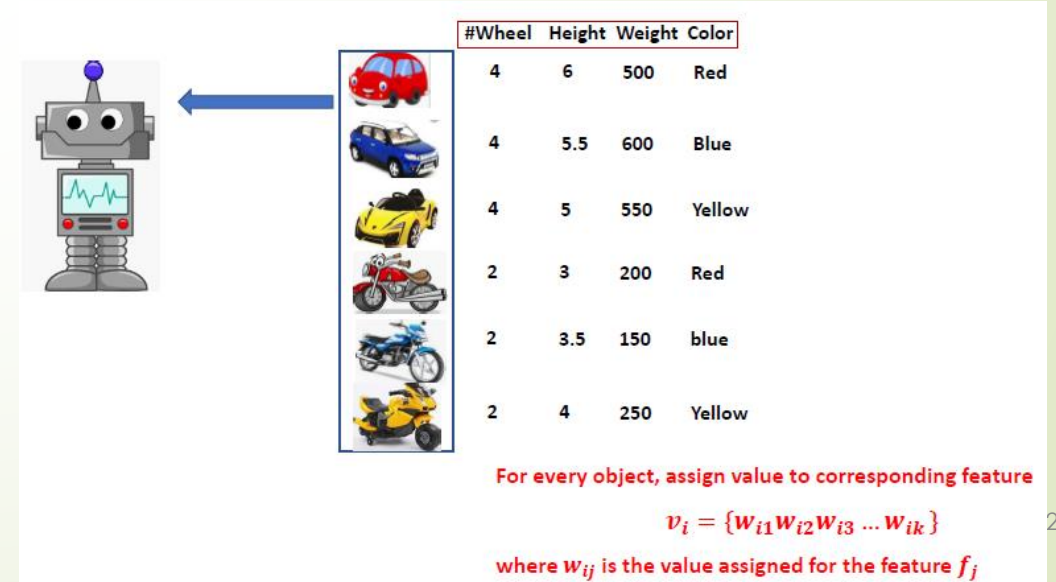
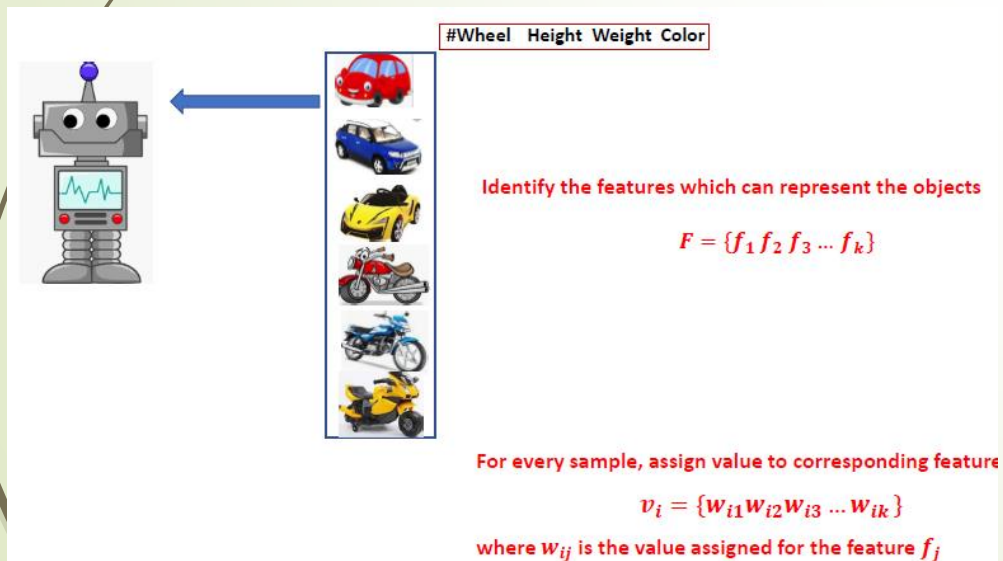
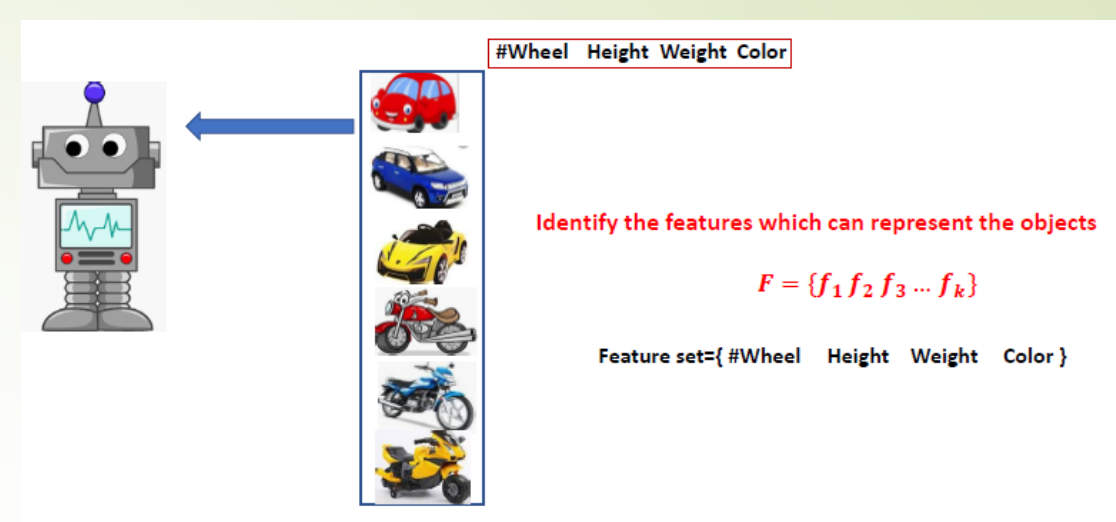
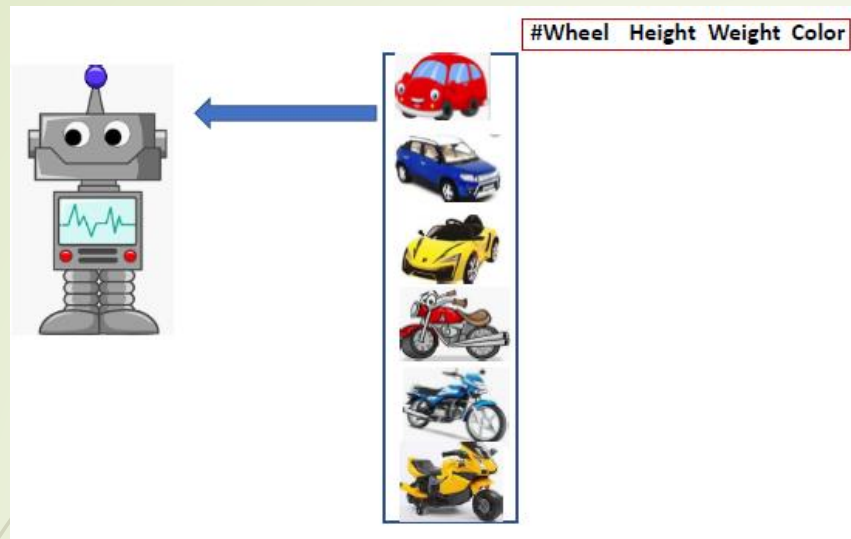
[The task is to identify the patterns like group the similar objects together]

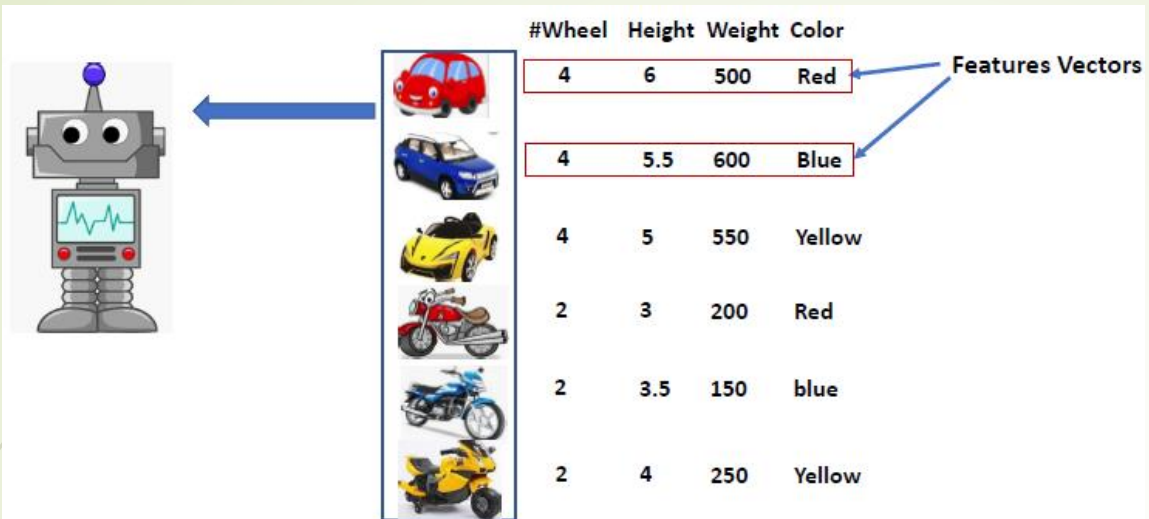
What is Reinforcement Learning



Teach a machine to identify vehicle types

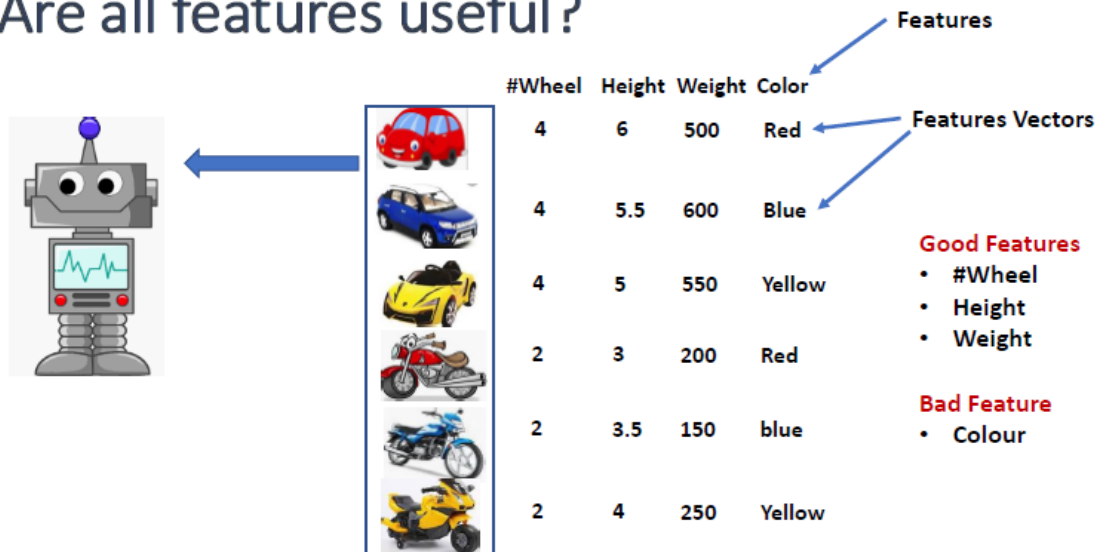


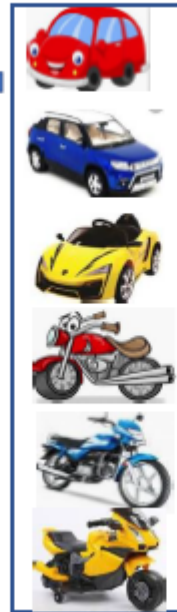
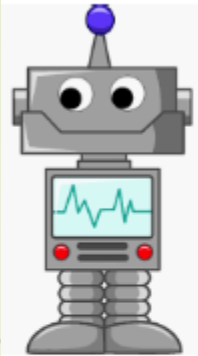




This form of representation is called **Vector Space Model**

Are all features useful?





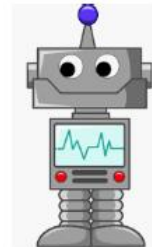
#Wheel Class Label

4	CAR
4	CAR
4	CAR
2	BIKE
2	BIKE
2	BIKE

Training Dataset

Feature vector with Class label

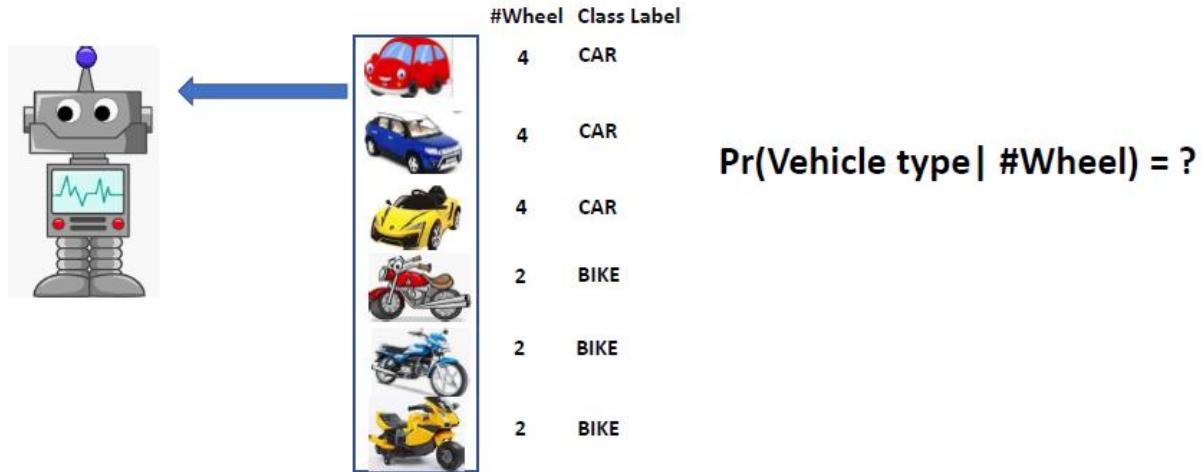
Given the #Wheel, identify the vehicle



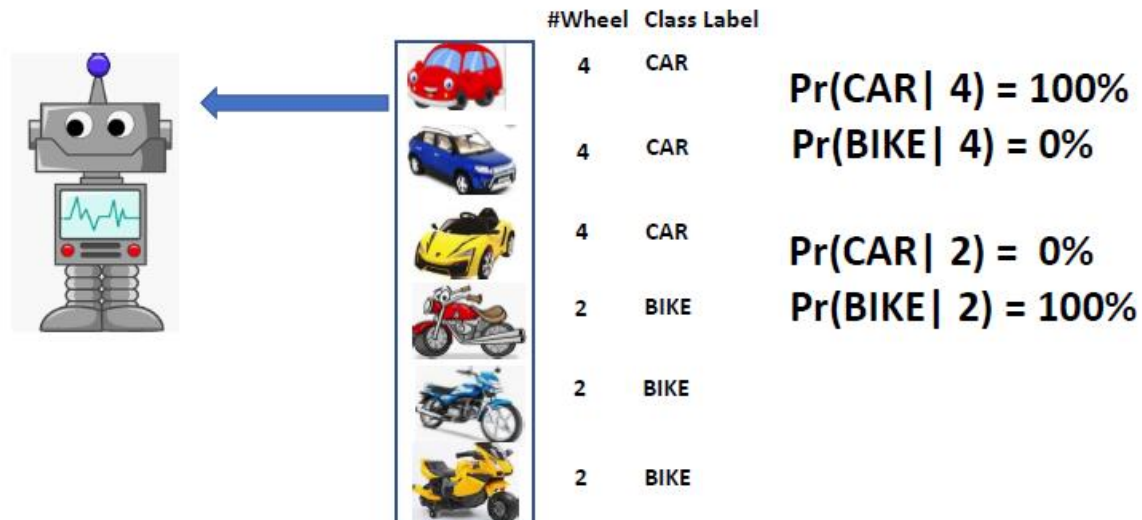
#Wheel Class Label

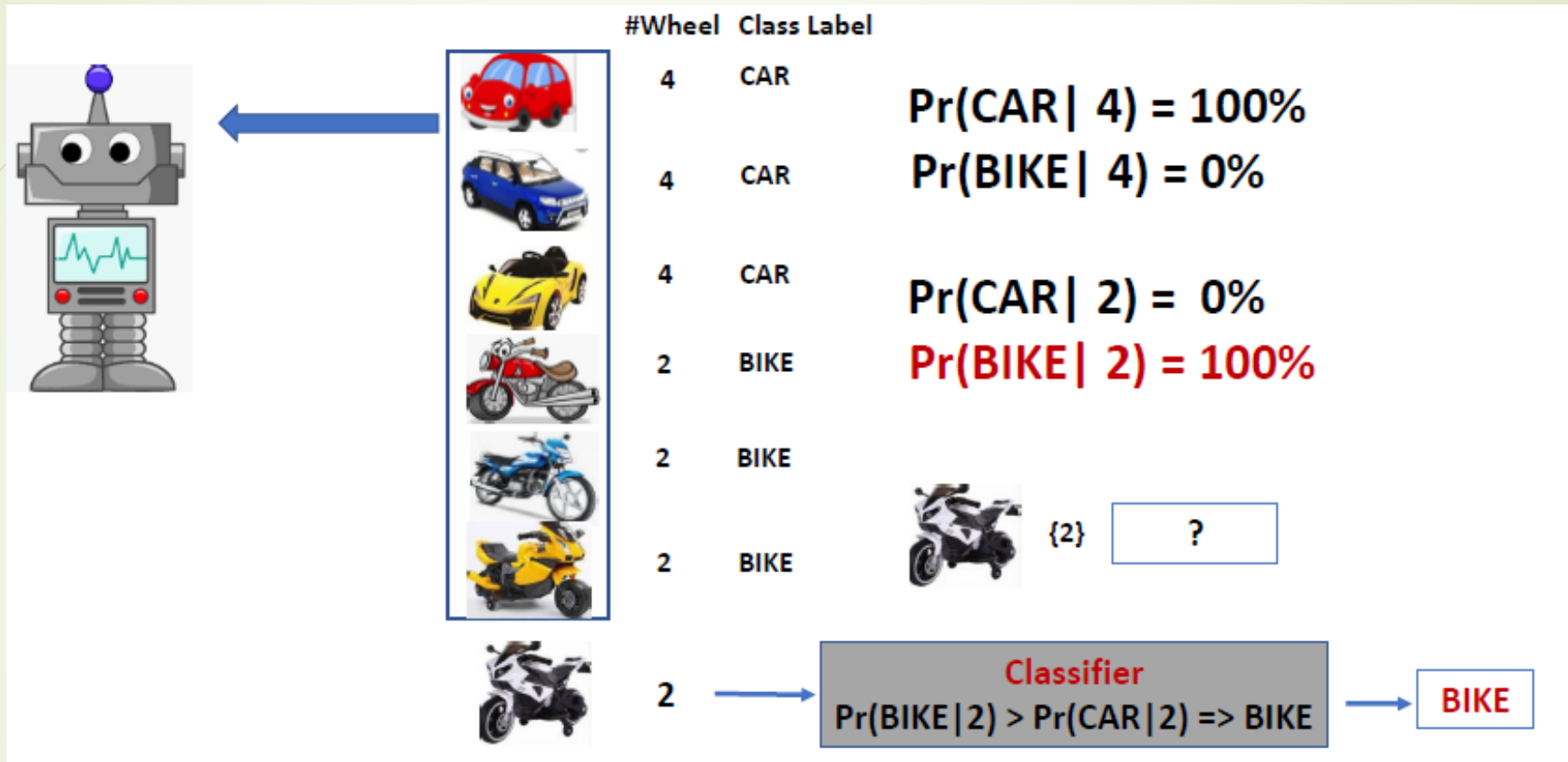
4	CAR
4	CAR
4	CAR
2	BIKE
2	BIKE
2	BIKE
2	?

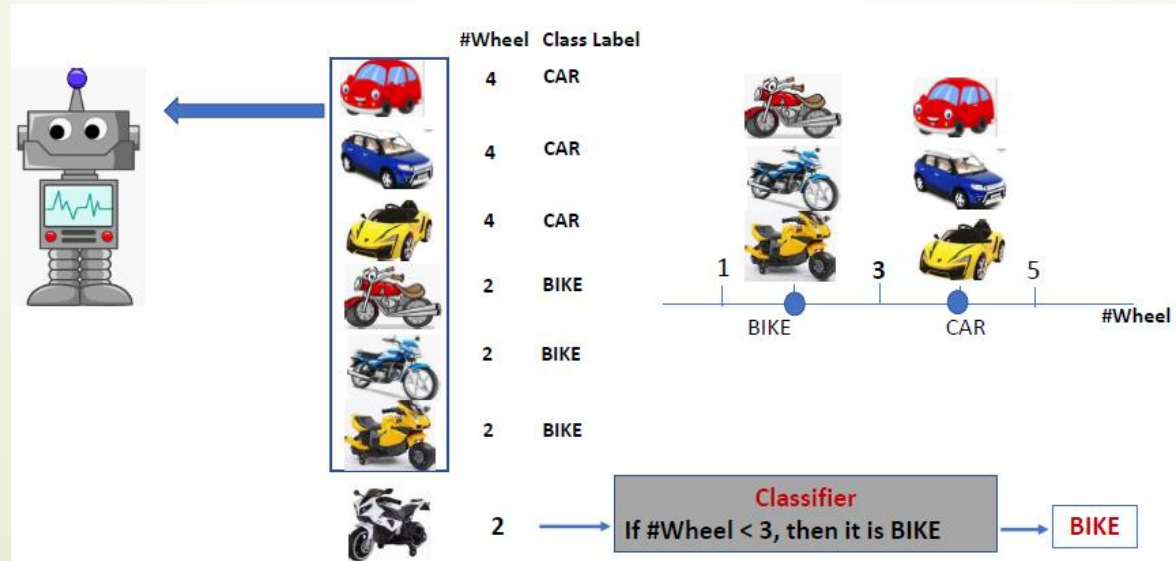
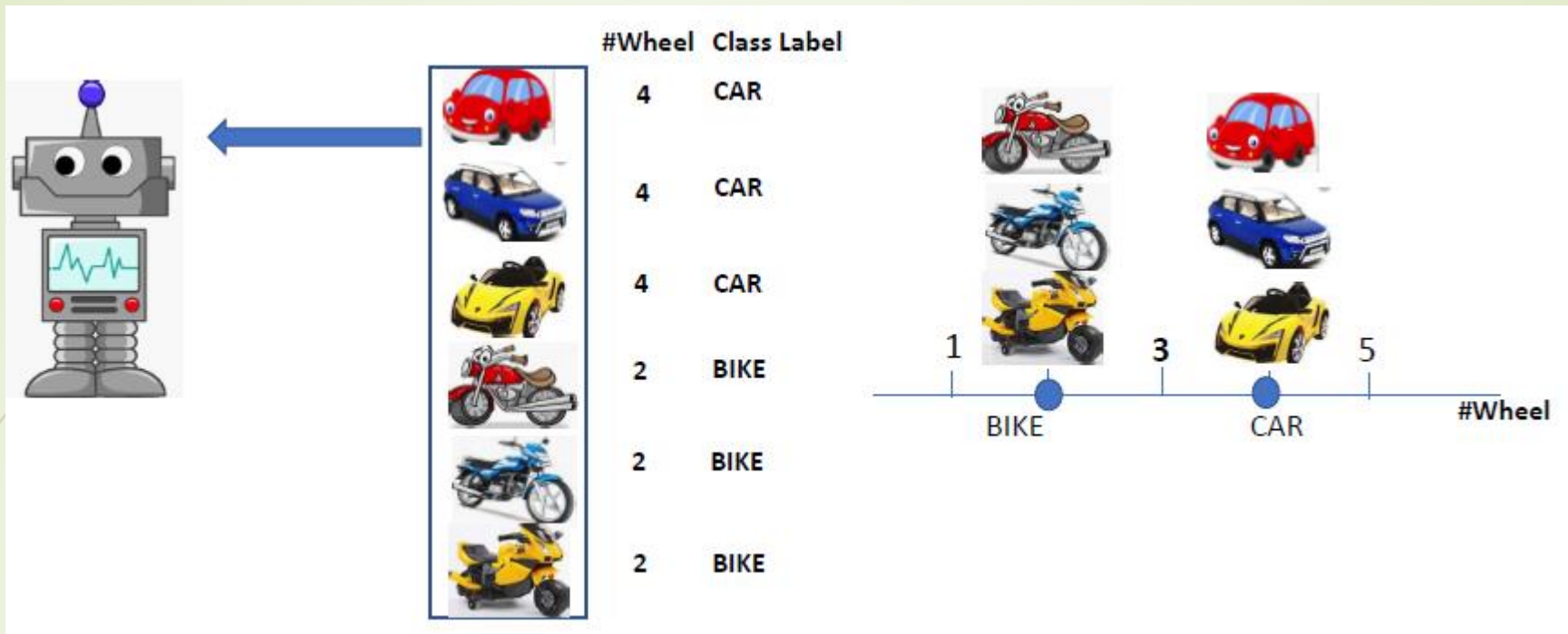
Let us estimate




Let us estimate the probability (type | #wheel)








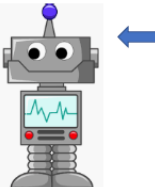


#Wheel	Class Label
4	CAR
4	CAR
4	CAR
2	BIKE
2	BIKE
2	BIKE
4	BIKE
2	CAR

$\Pr(\text{CAR} | 4) = 75\%$
 $\Pr(\text{BIKE} | 4) = 25\%$
 $\Pr(\text{CAR} | 2) = 25\%$
 $\Pr(\text{BIKE} | 2) = 75\%$




If selected feature is not sufficient




#Wheel	Class Label
4	CAR
4	CAR
4	CAR
2	BIKE
2	BIKE
2	BIKE
4	BIKE
2	CAR

$\Pr(\text{CAR} | 4) = 75\%$
 $\Pr(\text{BIKE} | 4) = 25\%$
 $\Pr(\text{CAR} | 2) = 25\%$
 $\Pr(\text{BIKE} | 2) = 75\%$



$\Pr(\text{BIKE} | 2) > \Pr(\text{CAR} | 2) \Rightarrow \text{BIKE}$


More Features



#Wheel	Height	Class Label
4	H	CAR
4	H	CAR
4	H	CAR
2	L	BIKE
2	L	BIKE
2	L	BIKE
4	L	BIKE
2	H	CAR


H: High, height ≥ 5
L: Low, height < 5

Estimate the probabilities, and ask the same question

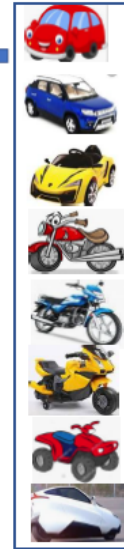
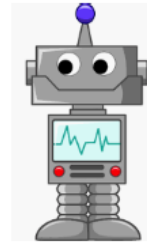


#Wheel	Height	Class Label
4	H	CAR
4	H	CAR
4	H	CAR
2	L	BIKE
2	L	BIKE
2	L	BIKE
4	L	BIKE
2	H	CAR

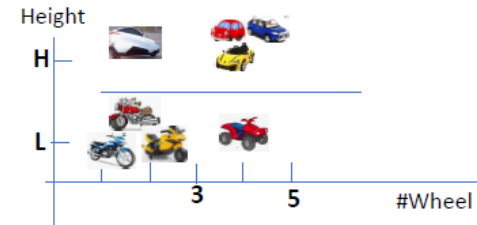
$\Pr(\text{CAR} \mid 4, H) = 100\%$
 $\Pr(\text{BIKE} \mid 4, L) = 100\%$
 $\Pr(\text{CAR} \mid 2, H) = 100\%$
 $\Pr(\text{BIKE} \mid 2, L) = 100\%$
 $\Pr(\text{CAR} \mid 4, L) = 0\%$
 $\Pr(\text{BIKE} \mid 4, H) = 0\%$
 $\Pr(\text{CAR} \mid 2, L) = 0\%$
 $\Pr(\text{BIKE} \mid 2, H) = 0\%$

 {2 H}

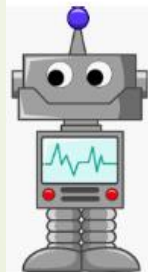
Multiple ways



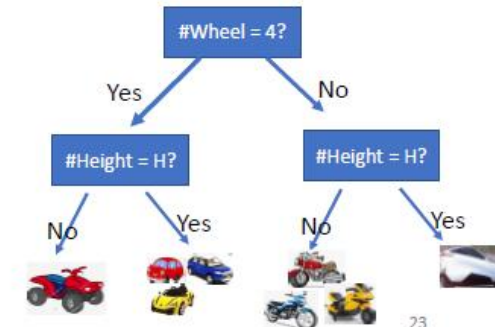
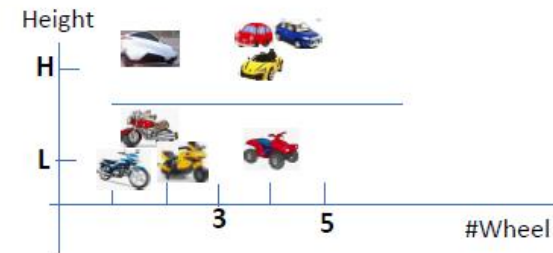
#Wheel	Height	Class Label
4	H	CAR
4	H	CAR
4	H	CAR
2	L	BIKE
2	L	BIKE
2	L	BIKE
4	L	BIKE
2	H	CAR



22



#Wheel	Height	Class Label
4	H	CAR
4	H	CAR
4	H	CAR
2	L	BIKE
2	L	BIKE
2	L	BIKE
4	L	BIKE
2	H	CAR



23

What is Classification?

	CAR
	CAR
	BIKE
	BIKE
Samples	Labels

Training Dataset

$$f(\text{Database}, \text{Car Image}) = \text{CAR/BIKE}$$

Classification

	CAR
	CAR
	BIKE
	BIKE
Samples	Labels

Training Dataset

$$f(\text{Database}, \text{Car Image}) = \text{CAR/BIKE}$$

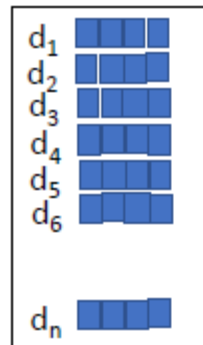
Given a dataset $D = \{x_1, x_2, x_3, \dots, x_n\}$ and set of class labels $C = \{c_1, c_2, c_3, \dots, c_k\}$, the task of classification is to devise a mapping function $f: D \rightarrow C$.

Classification

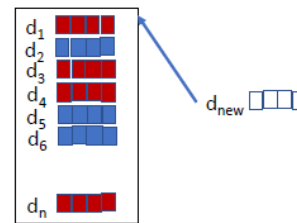
- Bayesian Classifier
- K-Nearest Neighbours
- Decision Tree
- Support Vector Machine
- Neural Network

k-Nearest Neighbors& Centroid Based Classifier

k-Nearest Neighbors



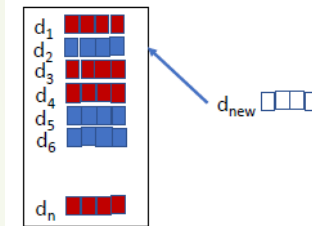
Dataset



Dataset

$$\omega(d_1, d_{new})$$

$$\text{Cosine Similarity}(d_j, d_{new}) = \frac{\sum_{i=1}^k (d_{ji} \cdot d_{newi})}{\sqrt{\sum_{i=1}^k d_{ji}^2} \sqrt{\sum_{i=1}^n d_{newi}^2}}$$

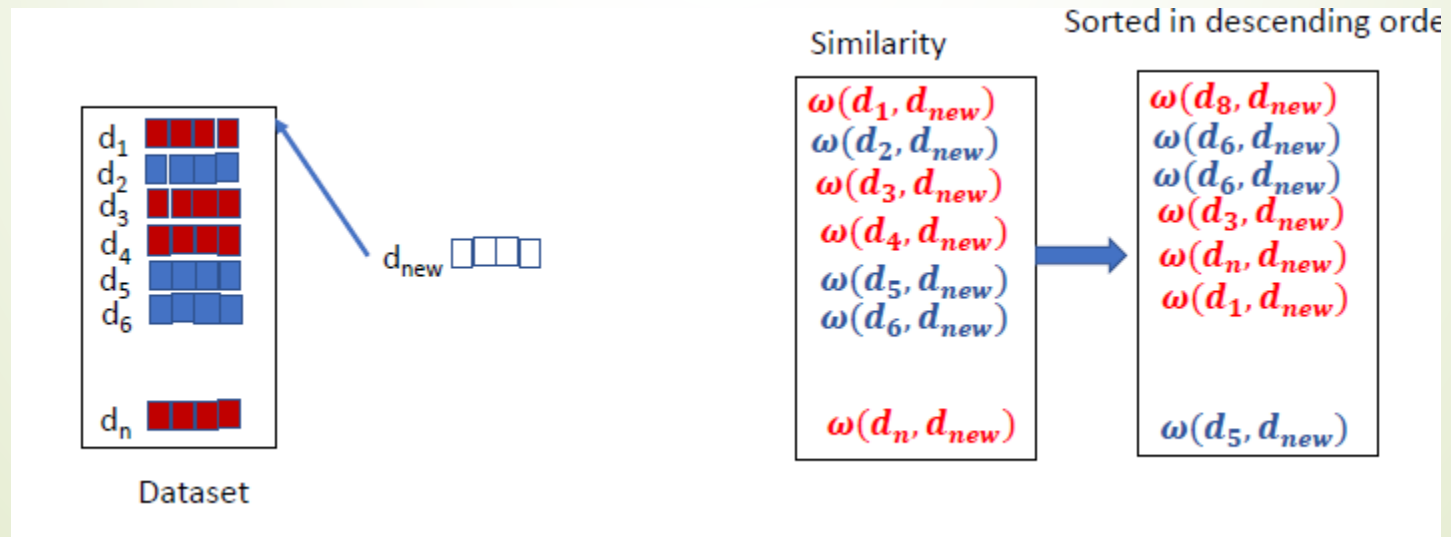
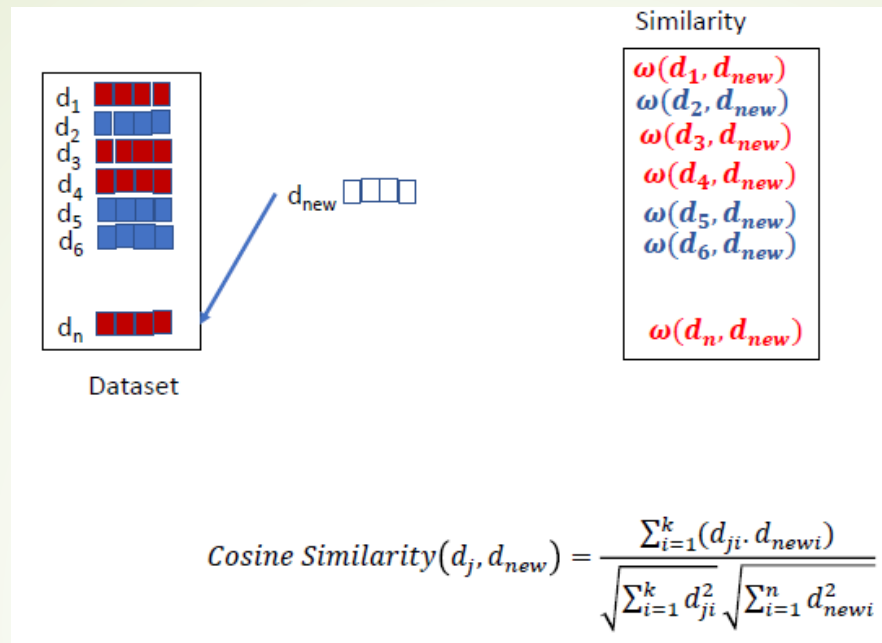


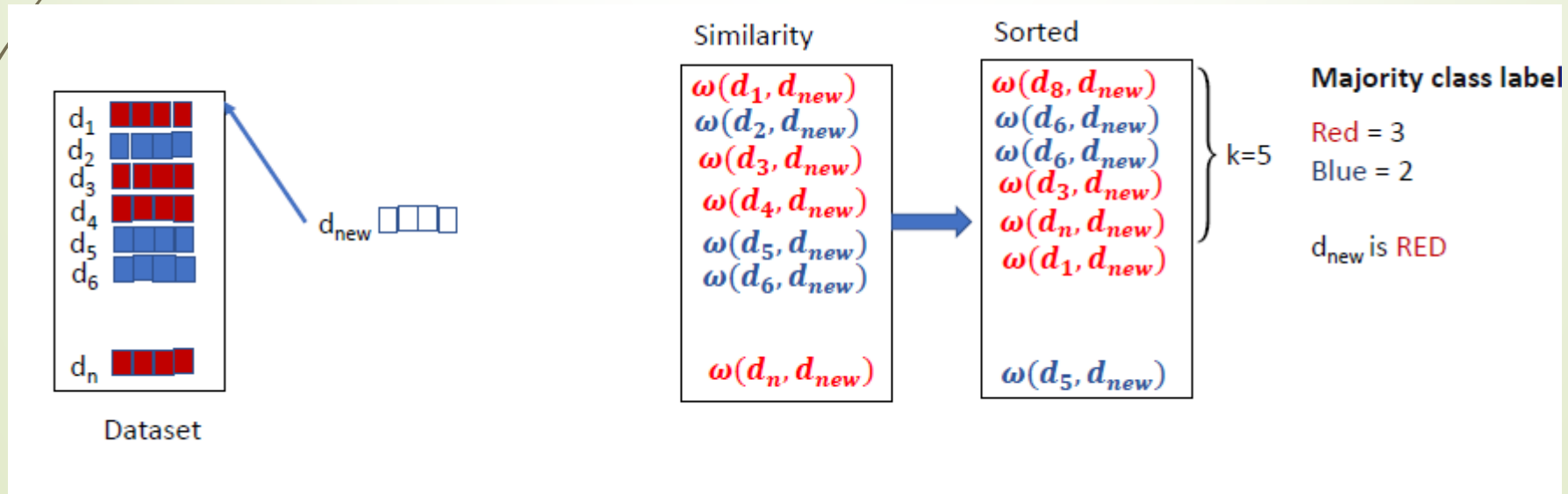
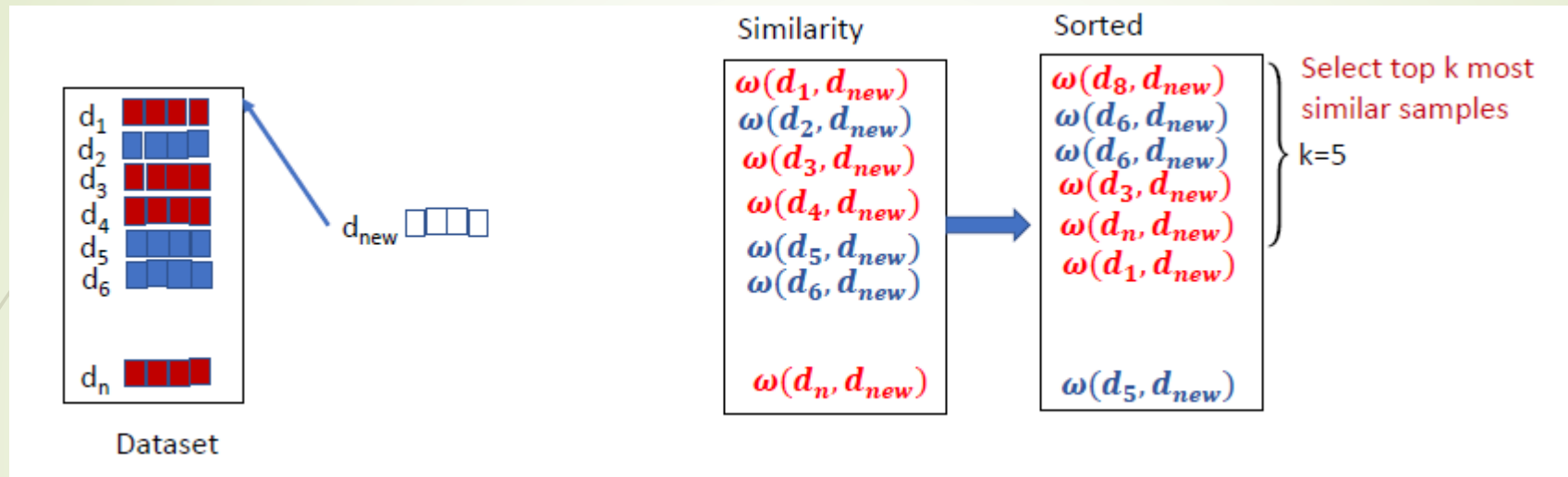
Dataset

$$\omega(d_1, d_{new})$$

$$\omega(d_2, d_{new})$$

$$\text{Cosine Similarity}(d_j, d_{new}) = \frac{\sum_{i=1}^k (d_{ji} \cdot d_{newi})}{\sqrt{\sum_{i=1}^k d_{ji}^2} \sqrt{\sum_{i=1}^n d_{newi}^2}}$$





Centroid Based Classifier

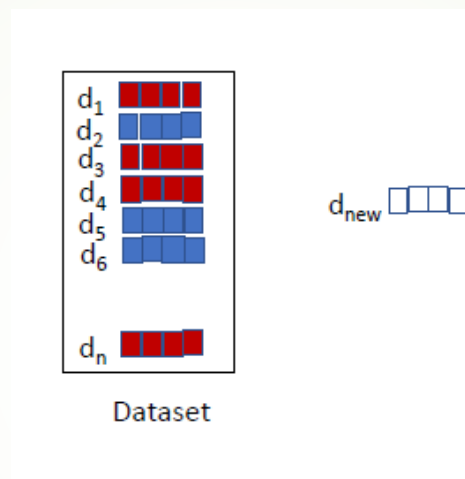
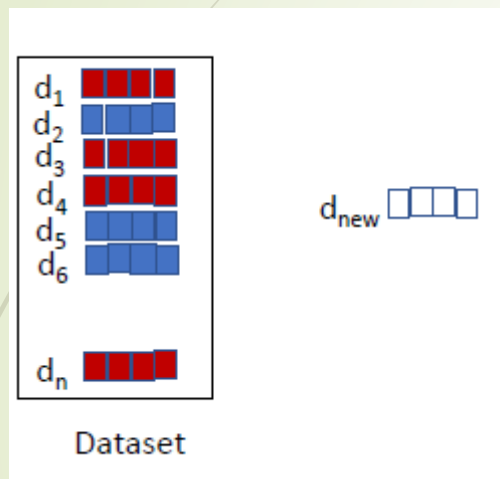
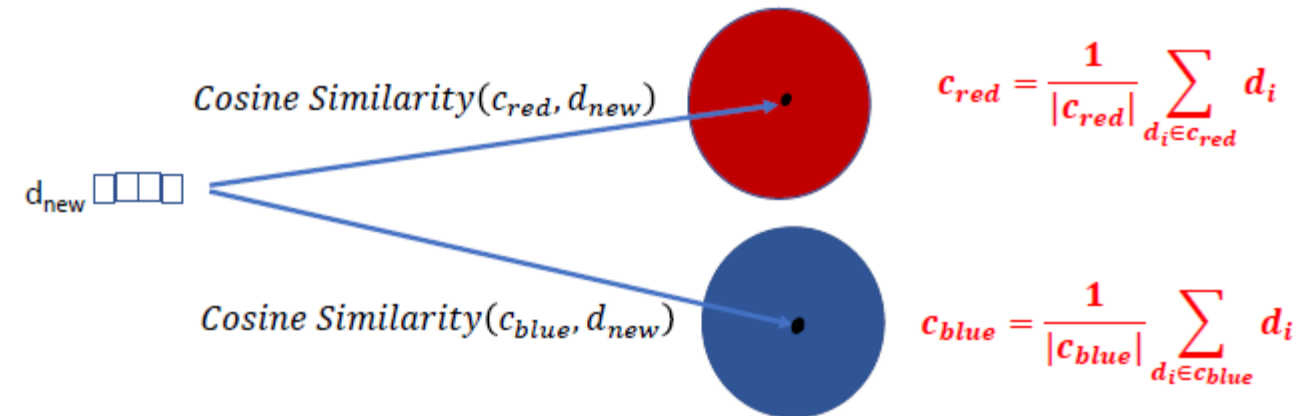
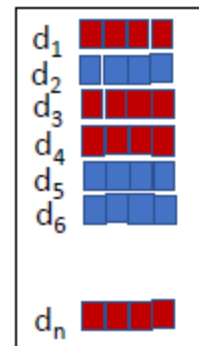
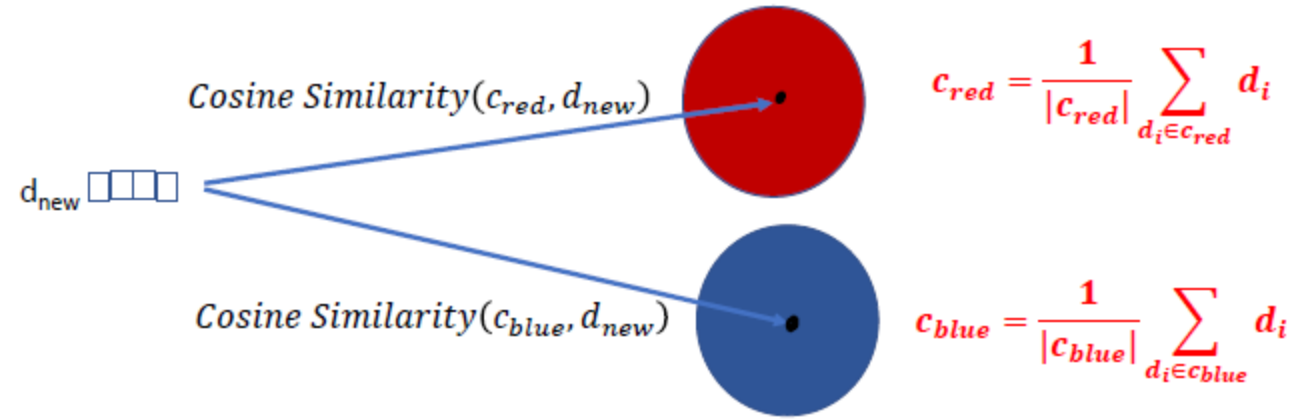
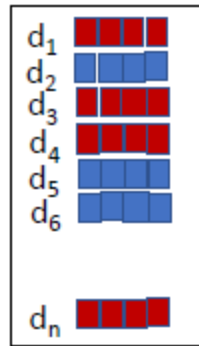


Diagram illustrating the calculation of centroids for two clusters. The red cluster is represented by a red circle with a black dot (centroid). The blue cluster is represented by a blue circle with a black dot (centroid).

$$c_{red} = \frac{1}{|c_{red}|} \sum_{d_i \in c_{red}} d_i$$

$$c_{blue} = \frac{1}{|c_{blue}|} \sum_{d_i \in c_{blue}} d_i$$



Assign Class Label with the nearest Centroid.

Decision Tree (Rule Based Approach)

Example

Features

outlook	temperature	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

outlook	temperature	humidity	windy	Class play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

outlook	temperature	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no

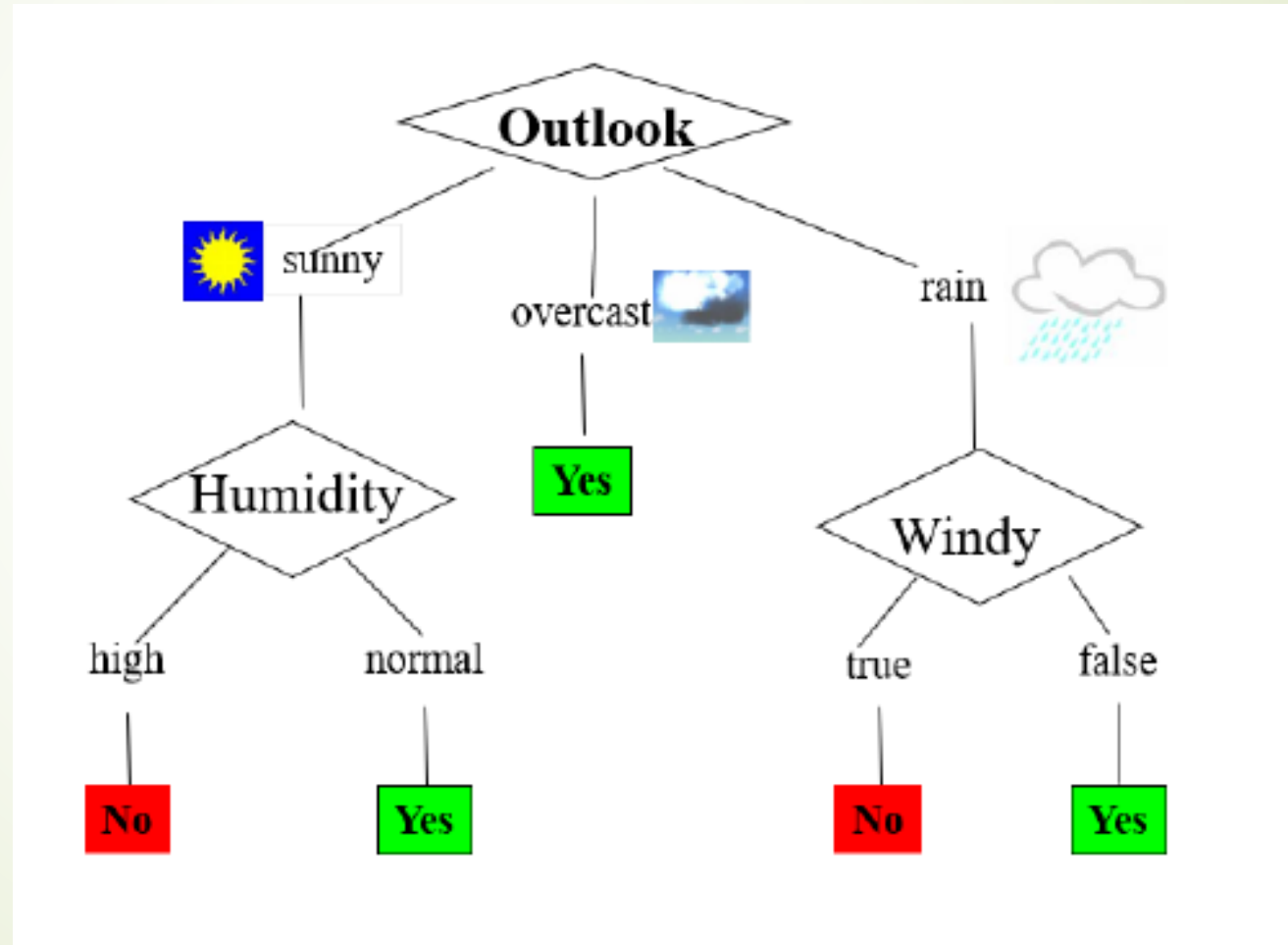
Given : <sunny, cool, high, true>

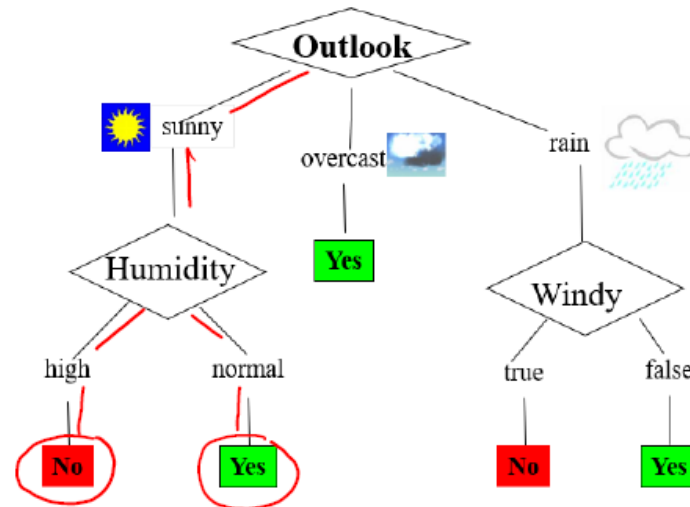
Predict, if there will be a match?

Assume that I have a set of rules:

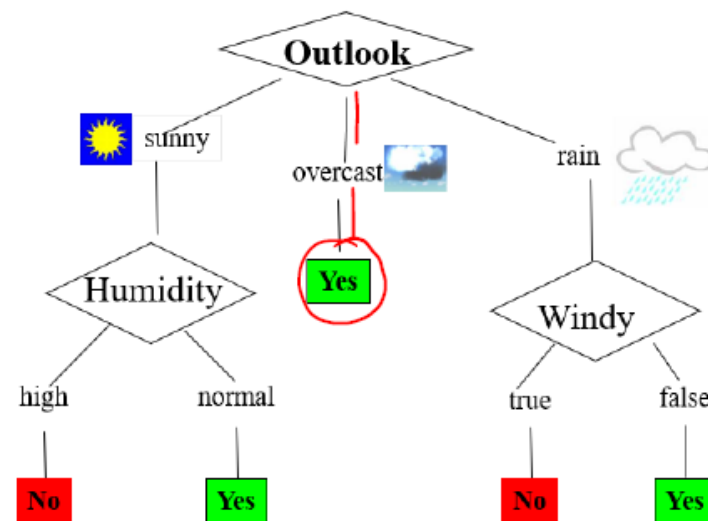
- If ((lookout=sunny) **and** (humudity=high) **and** (windy=false)) then (yes) else (no)
- If (lookout=overcast) then (yes)
- If ((lookout=sunny) **and** (humudity=high)) then (yes) else (no)
- so on.....

Set of rules can be visualized as a tree.



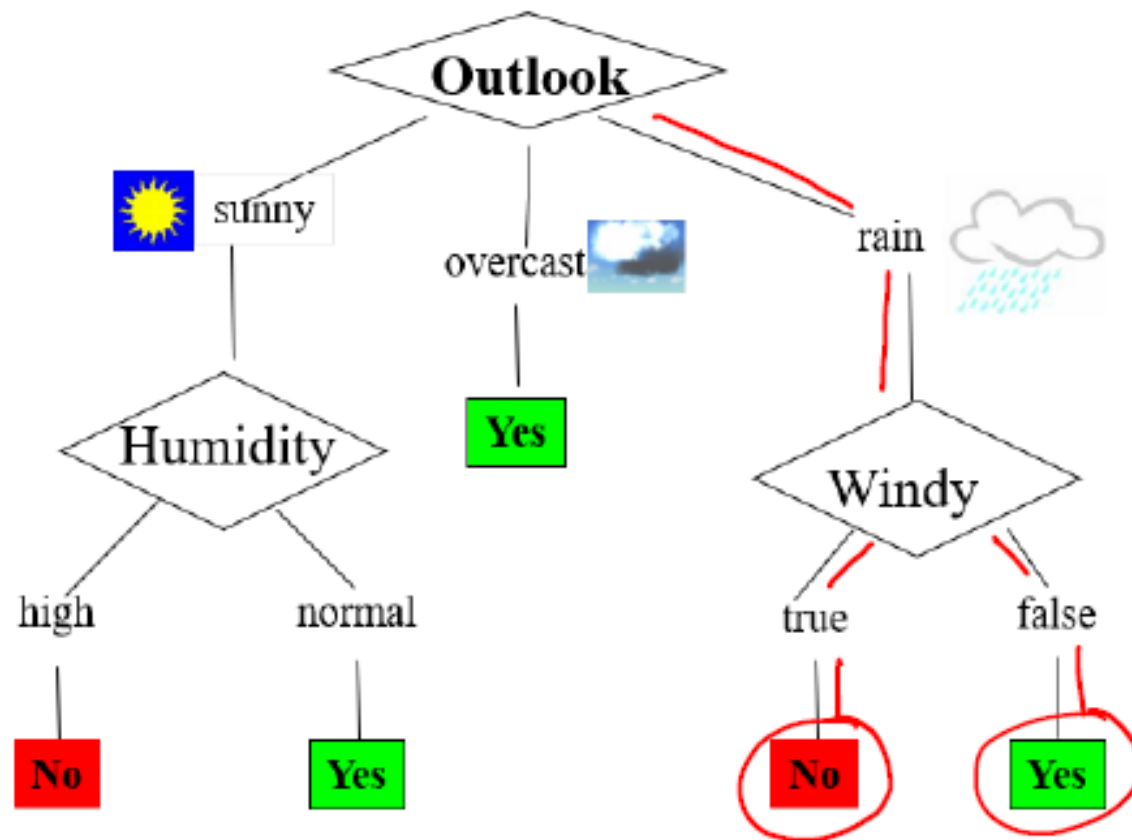


Rule 1: If ((lookout=sunny) **and** (humidity=high))
then (yes) else (no)



Rule 1: If ((lookout=sunny) **and** (humidity=high))
then (yes) else (no)

Rule 2: If (lookout=overcast) then (yes)



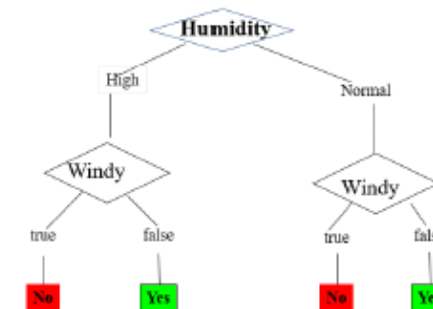
Rule 1: If ((lookout=sunny) **and** (humidity=high))
then (yes) else (no)

Rule 2: If (lookout=overcast) then (yes)

Rule 3: If ((lookout=rain) **and** (windy=true))
then (no) else (yes)

Many possible Trees

outlook	temperature	humidity	windy	play
sunny	hot	high	false	no
sunny	hot	high	true	no
overcast	hot	high	false	yes
rainy	mild	high	false	yes
rainy	cool	normal	false	yes
rainy	cool	normal	true	no
overcast	cool	normal	true	yes
sunny	mild	high	false	no
sunny	cool	normal	false	yes
rainy	mild	normal	false	yes
sunny	mild	normal	true	yes
overcast	mild	high	true	yes
overcast	hot	normal	false	yes
rainy	mild	high	true	no



Which Tree is the Best?

Models

80

➤ **“Traditional” Machine Learning**

- Support Vector Machines
- Decision Trees
- Random Forest
- ...

➤ **“Deep” Learning Methods**

- Neuronal Networks
- Convolutional Neuronal Networks
- Recurrent Neural Network (RNN)
- Generative Adversarial Network (GAN)
- ...

Models

81

- ▶ “Traditional” Machine Learning
 - ▶ Support Vector Machines
 - ▶ Decision Trees
 - ▶ Random Forest
 - ▶ ...
- ▶ “Deep” Learning Methods
 - ▶ Neuronal Networks
 - ▶ Convolutional Neuronal Networks
 - ▶ Recurrent Neural Network (RNN)
 - ▶ Generative Adversarial Network (GAN)
 - ▶ ...

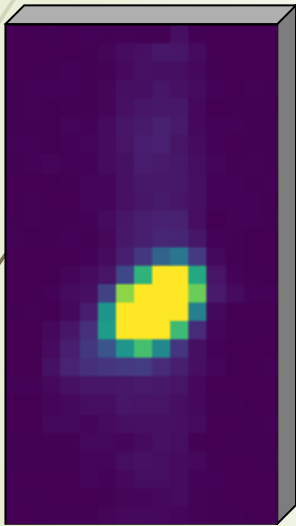
We will look at some of them in this lecture.

We will focus mainly on Deep Learning Methods.

Example

82

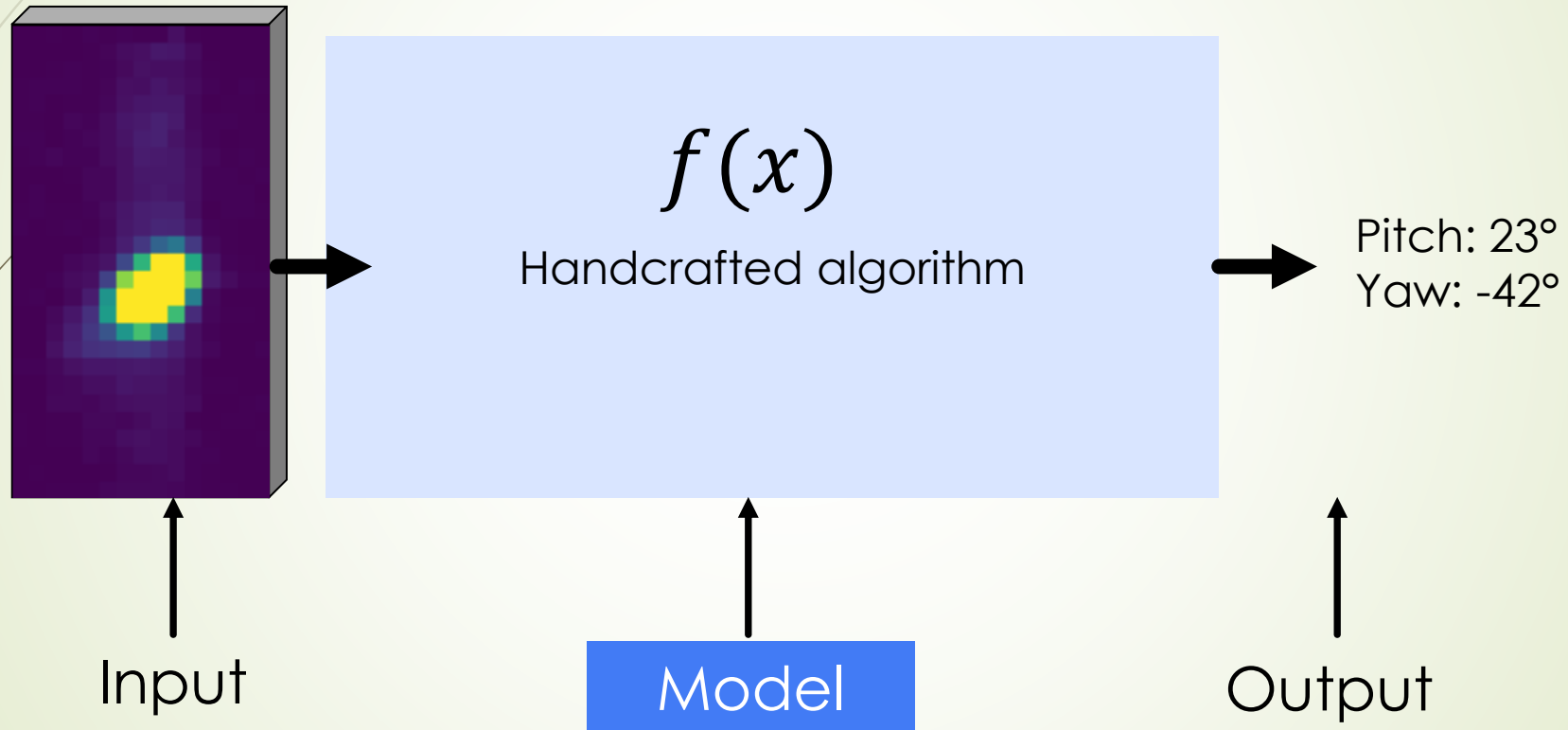
Human-Computer Interaction



Example

83

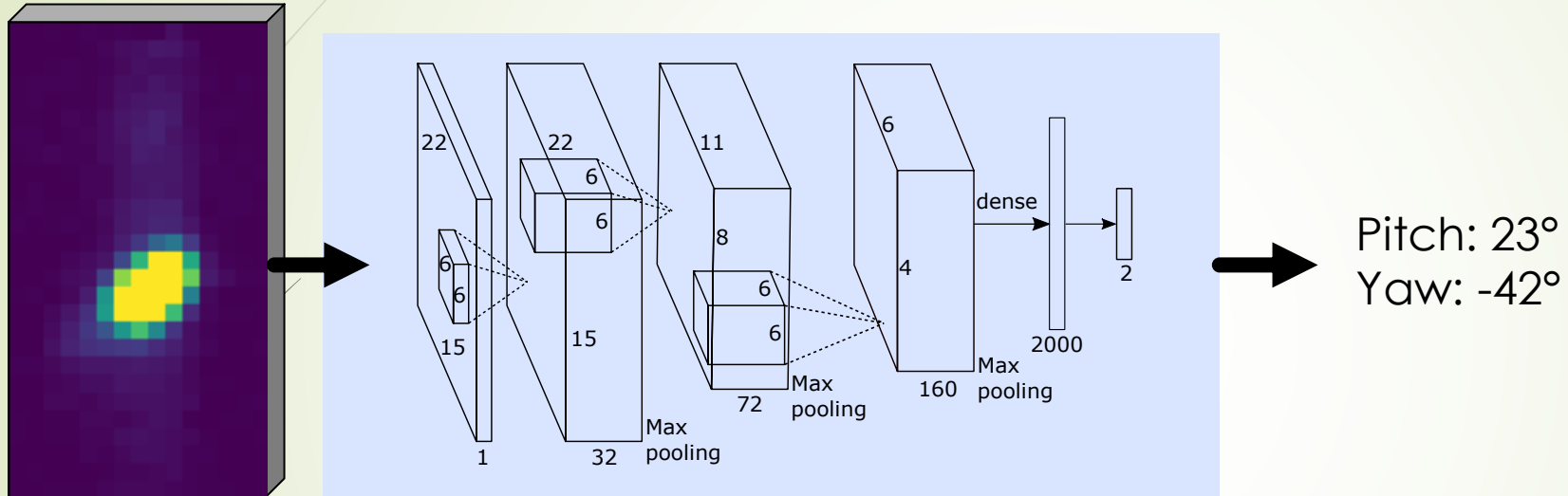
Human-Computer Interaction



Example

84

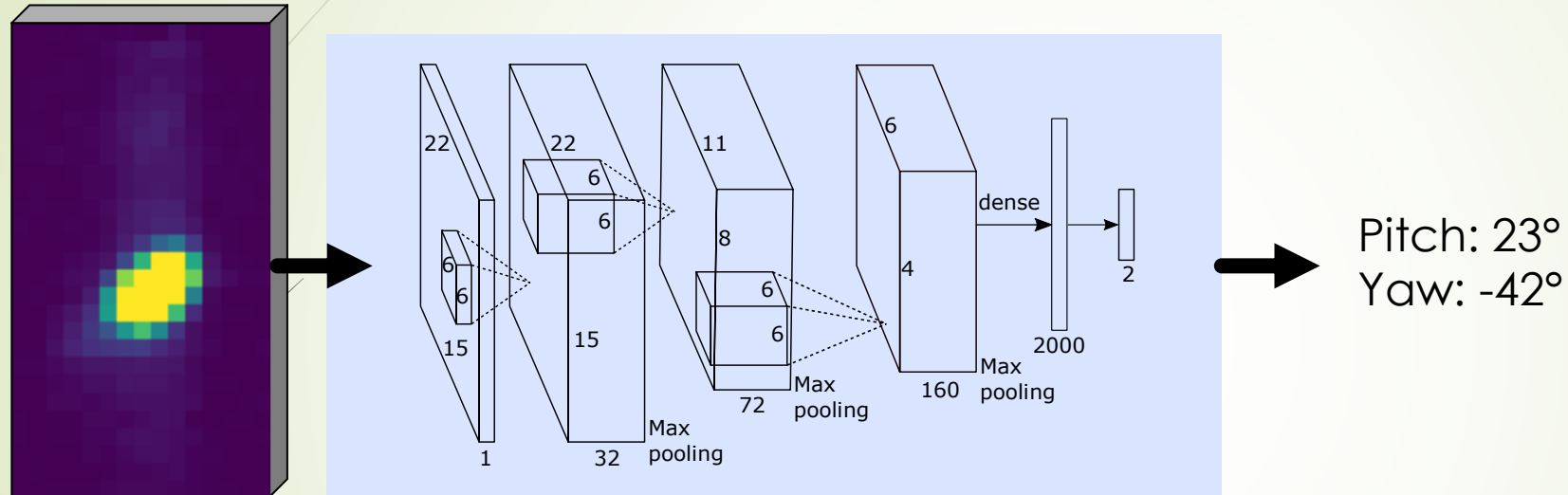
Human-Computer Interaction



Example

85

Human-Computer Interaction



Method	Pitch			Yaw		
	RMSE	MAE	SD	RMSE	MAE	SD
<i>GP reimplementation of Xiao et al. [41]*</i>	14.74	11.78	14.38	56.58	40.51	39.51
<i>pseudo implementation of Xiao et al. [41]**</i>	14.19	11.58	8.21	44.53	33.39	29.46
CNN + L2	12.8	10.09	7.88	24.19	17.62	16.58

8.9%

45.7%

Neuronal Networks

86

What can be trained?

Psychological Review
Vol. 65, No. 6, 1958

THE PERCEPTRON: A PROBABILISTIC MODEL FOR INFORMATION STORAGE AND ORGANIZATION IN THE BRAIN¹

F. ROSENBLATT

Cornell Aeronautical Laboratory

If we are eventually to understand the capability of higher organisms for perceptual recognition, generalization, recall, and thinking, we must first have answers to three fundamental

and the stored pattern. According to this hypothesis, if one understood the code or "wiring diagram" of the nervous system, one should, in principle, be able to discover exactly what an

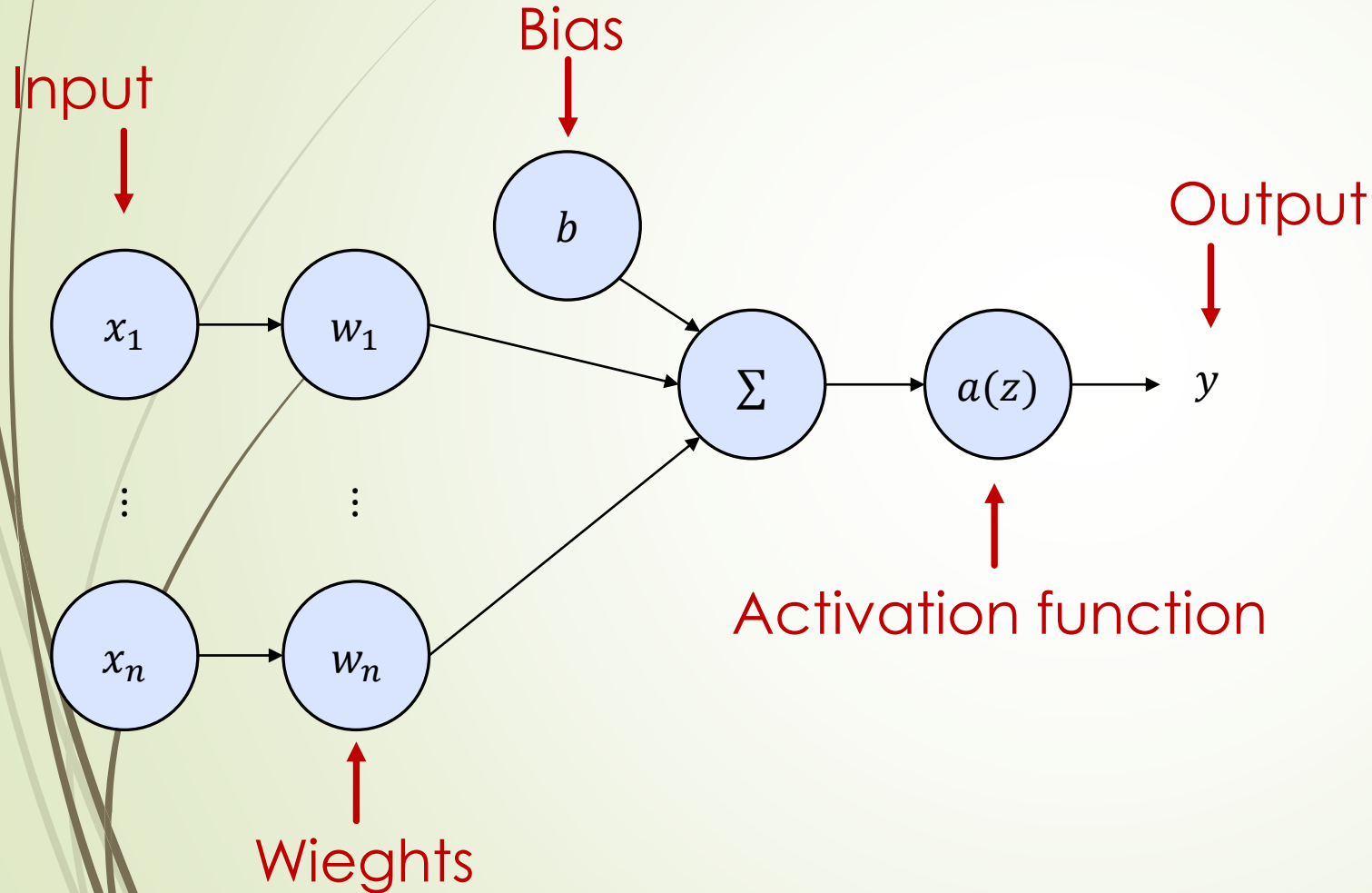
Frank Rosenblatt. "The perceptron: a probabilistic model for information storage and organization in the brain." *Psychological review* 65, no. 6 (1958): 386. DOI: <https://psycnet.apa.org/doi/10.1037/h0042519>

Sven Mayer

What is a Perceptron?

87

Single-Layer Perceptron



	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

$\Pr(\text{CAR} \mid 4, \text{H}) = 100\%$
 $\Pr(\text{BIKE} \mid 4, \text{L}) = 100\%$
 $\Pr(\text{CAR} \mid 2, \text{H}) = 100\%$
 $\Pr(\text{BIKE} \mid 2, \text{L}) = 100\%$
 $\Pr(\text{CAR} \mid 4, \text{L}) = 0\%$
 $\Pr(\text{BIKE} \mid 4, \text{H}) = 0\%$
 $\Pr(\text{CAR} \mid 2, \text{L}) = 0\%$
 $\Pr(\text{BIKE} \mid 2, \text{H}) = 0\%$



{2 H}

?

$$\Pr(c_i|x), \forall c_i \in \mathcal{C}$$

$$\text{class} = \arg \max_{c_i} \Pr(c_i|x)$$

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

$\Pr(\text{CAR} \mid 4, H) = 100\%$

$\Pr(\text{BIKE} \mid 4, L) = 100\%$

$\Pr(\text{CAR} \mid 2, H) = 100\%$

$\Pr(\text{BIKE} \mid 2, L) = 100\%$

$\Pr(\text{CAR} \mid 4, L) = 0\%$

$\Pr(\text{BIKE} \mid 4, H) = 0\%$

$\Pr(\text{CAR} \mid 2, L) = 0\%$

$\Pr(\text{BIKE} \mid 2, H) = 0\%$



{2 H}

?

$\Pr(c_i \mid x), \forall c_i \in \mathcal{C}$

$\text{class} = \arg \max_{c_i} \Pr(c_i \mid x)$

$\Pr(\text{CAR} \mid \text{img})$

$\Pr(\text{CAR} \mid \{2, H\}) = 1$

$\Pr(\text{BIKE} \mid \{2, H\}) = 0$

$\text{class} = \text{CAR}$

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR









$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$









prior

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

13

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

2








	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

Likelihood









2

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

2









	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

Evidence

Σ

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR









Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

$$= \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x|c_1) \Pr(c_1) + \Pr(x|c_2) \Pr(c_2) + \dots + \Pr(x|c_k) \Pr(c_k)}$$

Marginalization

Σ

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR




Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

Posterior

3

⇒ CAR

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

Bayes Rule

$$\Pr(c_i|x) = \frac{\Pr(c_i, x)}{\Pr(x)} = \frac{\Pr(x|c_i) \Pr(c_i)}{\Pr(x)}$$

Posterior
In Bayesian classification
we estimate Posterior
of a class given a sample.

3

⇒ CAR

	#Wheel	Height	Class Label
	4	H	CAR
	4	H	CAR
	4	H	CAR
	2	L	BIKE
	2	L	BIKE
	2	L	BIKE
	4	L	BIKE
	2	H	CAR

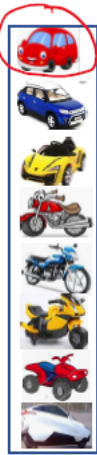
$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗}) = \Pr(CAR | \{4, H\}) = \frac{\Pr(\{4, H\} | CAR) \Pr(CAR)}{\Pr(\{4, H\})}$$

$$= \frac{0.75 \times 0.5}{0.375} = 1$$

$$\Pr(BIKE | \text{🚗}) = \Pr(BIKE | \{4, H\}) = \frac{\Pr(\{4, H\} | BIKE) \Pr(BIKE)}{\Pr(\{4, H\})}$$

$$= \frac{0 \times 0.5}{0.375} = 0$$



#	Wheel	Height	Class	Label
4	H	CAR		
4	H	CAR		
4	H	CAR		
2	L	BIKE		
2	L	BIKE		
2	L	BIKE		
4	L	BIKE		
2	H	CAR		

22

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗}) = \Pr(CAR | \{4, H\}) = \frac{\Pr(\{4, H\} | CAR) \Pr(CAR)}{\Pr(\{4, H\})}$$

$$= \frac{0.75 \times 0.5}{0.375} = 1$$

$$\Pr(BIKE | \text{🚗}) = \Pr(BIKE | \{4, H\}) = \frac{\Pr(\{4, H\} | BIKE) \Pr(BIKE)}{\Pr(\{4, H\})}$$

$$= \frac{0 \times 0.5}{0.375} = 0$$

1 CAR



#	Wheel	Height	Class	Label
4	H	CAR		
4	H	CAR		
4	H	CAR		
2	L	BIKE		
2	L	BIKE		
2	L	BIKE		
4	L	BIKE		
2	H	CAR		

23

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗})$$

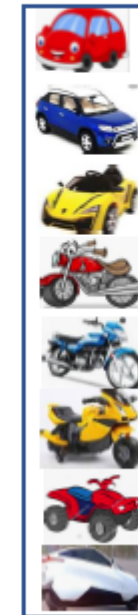
$$= \Pr(CAR | \{4, H\})$$

$$= \frac{\Pr(\{4, H\} | CAR) \Pr(CAR)}{\Pr(\{4, H\})}$$

$$\Pr(BIKE | \text{🏍️})$$

$$= \Pr(BIKE | \{4, H\})$$

$$= \frac{\Pr(\{4, H\} | BIKE) \Pr(BIKE)}{\Pr(\{4, H\})}$$



#WheelHeightClass Label

4 H CAR

4 H CAR

4 H CAR

2 L BIKE

2 L BIKE

2 L BIKE

4 L BIKE

2 H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗})$$

$$= \Pr(CAR | \{4, H\})$$

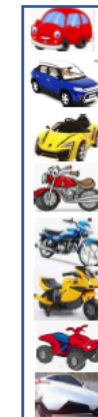
$$= \frac{\Pr(\{4, H\} | CAR) \Pr(CAR)}{\Pr(\{4, H\})}$$

$$\Pr(BIKE | \text{🏍️})$$

$$= \Pr(BIKE | \{4, H\})$$

$$= \frac{\Pr(\{4, H\} | BIKE) \Pr(BIKE)}{\Pr(\{4, H\})}$$

← Same →



#WheelHeightClass Label

4 H CAR

4 H CAR

4 H CAR

2 L BIKE

2 L BIKE

2 L BIKE

4 L BIKE

2 H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗})$$

$$= \Pr(CAR | \{4, H\})$$







$$\sim \Pr(\{4, H\} | CAR) \Pr(CAR)$$

$$\Pr(BIKE | \text{🚗})$$

$$= \Pr(BIKE | \{4, H\})$$

$$\sim \Pr(\{4, H\} | BIKE) \Pr(BIKE)$$

Relation still maintains

#WheelHeightClass Label		
	4	H CAR
	4	H CAR
	4	H CAR
	2	L BIKE
	2	L BIKE
	2	L BIKE
	4	L BIKE
	2	H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2 w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2 w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2 w_3 \dots w_k\})}$$

$$\Pr(CAR | \text{🚗})$$

$$= \Pr(CAR | \{4, H\})$$


$$\sim \Pr(\{4, H\} | CAR) \Pr(CAR)$$

$$\Pr(BIKE | \text{🚗})$$

$$= \Pr(BIKE | \{4, H\})$$






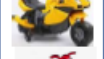


$$\sim \Pr(\{4, H\} | BIKE) \Pr(BIKE)$$

Relation still maintains

#WheelHeightClass Label		
	4	H CAR
	4	H CAR
	4	H CAR
	2	L BIKE
	2	L BIKE
	2	L BIKE
	4	L BIKE
	2	H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$


If k (the number of classes) is **small**,

#WheelHeightClass Label		
	4	H CAR
	4	H CAR
	4	H CAR
	2	L BIKE
	2	L BIKE
	2	L BIKE
	4	L BIKE
	2	H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

If k (the number of classes) is **small**,

estimating **likelihood** $\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i)$ is **feasible**.

#WheelHeightClass Label		
	4	H CAR
	4	H CAR
	4	H CAR
	2	L BIKE
	2	L BIKE
	2	L BIKE
	4	L BIKE
	2	H CAR

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

However, if **k** (the number of classes) is **very large**,

estimating **likelihood** $\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i)$ is **a very expensive task** over **a large dataset**.

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

However, if **k** (the number of classes) is **very large**,

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$$\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) = \Pr(w_1 | w_2, w_3, \dots, w_k, c_i) \cdot \Pr(w_2 | w_3, w_4, \dots, w_k, c_i) \dots \Pr(w_k | c_i)$$

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

However, if **k** (the number of classes) is **very large**,

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$$\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) = \underbrace{\Pr(w_1 | w_2, w_3, \dots, w_k, c_i)} \cdot \underbrace{\Pr(w_2 | w_3, w_4, \dots, w_k, c_i)} \dots \underbrace{\Pr(w_k | c_i)}$$

Naïve Bayes Classifier

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

To simplify the estimation, we make an **assumption**

- The features are **conditionally independent**.

Naïve Bayes Classifier

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

To simplify the estimation, we make an **assumption**

- The features are **conditionally independent**.

$$\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) = \Pr(w_1 | w_2, w_3, \dots, w_k, c_i) \Pr(w_2 | w_3, w_4, \dots, w_k, c_i) \dots \Pr(w_k | c_i)$$

$\overset{= \Pr(w_1 | c_i)}{\circlearrowleft}$
 $\overset{= \Pr(w_2 | c_i)}{\circlearrowleft}$

Naïve Bayes Classifier

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

To simplify the estimation, we make an **assumption**

- The features are **conditionally independent**.

Bayesian: $\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) = \Pr(w_1 | w_2, w_3, \dots, w_k, c_i) \cdot \Pr(w_2 | w_3, w_4, \dots, w_k, c_i) \dots \Pr(w_k | c_i)$

Naïve Bayes: $\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \sim \Pr(w_1 | c_i) \cdot \Pr(w_2 | c_i) \dots \Pr(w_k | c_i) = \prod_{j=1}^k \Pr(w_j | c_i)$

Naïve Bayes Classifier

$$\Pr(c_i|x) = \Pr(c_i | \{w_1, w_2, w_3 \dots w_k\}) = \frac{\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \Pr(c_i)}{\Pr(\{w_1, w_2, w_3 \dots w_k\})}$$

#Wheel	Height	Class	Label
4	H	CAR	
4	H	CAR	
4	H	CAR	
2	L	BIKE	
2	L	BIKE	
2	L	BIKE	
4	L	BIKE	
2	H	CAR	

$$\sim \prod_{j=1}^k \Pr(w_j | c_i) \Pr(c_i)$$

$$\Pr(CAR | \{4, H\}) = \Pr(4|CAR) \times \Pr(H|CAR) \times \Pr(CAR)$$

$$= 0.75 \times 1 \times 0.5 = 0.375$$

$$\Pr(BIKE | \{4, H\}) = \Pr(4|BIKE) \times \Pr(H|BIKE) \times \Pr(BIKE)$$

$$= 0.25 \times 0 \times 0.5 = 0$$

CAR

39

What is one of the estimate in the **likelihood** is zero?

$$\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \sim \Pr(w_1 | c_i) \cdot \Pr(w_2 | c_i) \dots \Pr(w_k | c_i) = \prod_{j=1}^k \Pr(w_j | c_i)$$

$$\Pr(CAR | \{4, M\}) = \Pr(4|CAR) \times \Pr(M|CAR) \times \Pr(CAR)$$

$$= 0.75 \times 0 \times 0.5 = 0$$

What is one of the estimate in the **likelihood** is zero?

$$\Pr(\{w_1, w_2, w_3 \dots w_k\} | c_i) \sim \Pr(w_1 | c_i) \cdot \Pr(w_2 | c_i) \dots \Pr(w_k | c_i) = \prod_{j=1}^k \Pr(w_j | c_i)$$

$$\begin{aligned} \Pr(CAR | \{4, \mathbf{M}\}) &= \Pr(4 | CAR) \times \Pr(M | CAR) \times \Pr(CAR) \\ &= 0.75 \times 0 \times 0.5 = 0 \end{aligned}$$

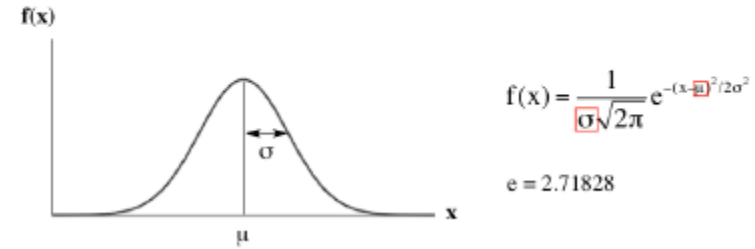
Smoothing $\Pr(M | CAR) = \frac{0 + \text{Small}}{|CAR| + \text{Large}}$

In some of the machine learning tools, you may find

- Naïve Bayes with **Gaussian**
- Naïve Bayes with **Multinomial**

In some of the machine learning tools, you may find

- Naïve Bayes with **Gaussian**



In some of the machine learning tools, you may find

- Naïve Bayes with **Multinomial** $f(x_1, \dots, x_k; n, p_1, \dots, p_k) = \Pr(X_1 = x_1 \text{ and } \dots \text{ and } X_k = x_k)$

$$= \begin{cases} \frac{n!}{x_1! \dots x_k!} p_1^{x_1} \dots p_k^{x_k}, & \text{when } \sum_{i=1}^k x_i = n \\ 0 & \text{otherwise,} \end{cases}$$

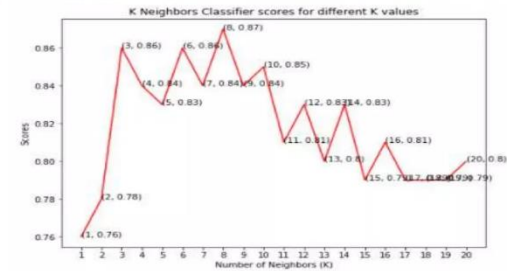
K Neighbors Classifier

This classifier looks for the classes of K nearest neighbors of a given data point and based on the majority class, it assigns a class to this data point. However, the number of neighbors can be varied. I varied them from 1 to 20 neighbors and calculated the test score in each case.

```
In [19]: knn_scores = []
for k in range(1,21):
    knn_classifier = KNeighborsClassifier(n_neighbors = k)
    knn_classifier.fit(X_train, y_train)
    knn_scores.append(knn_classifier.score(X_test, y_test))
```

Then, I plot a line graph of the number of neighbors and the test score achieved in each case.

```
In [20]: plt.plot([k for k in range(1, 21)], knn_scores, color = 'red')
for i in range(1,21):
    plt.text(i, knn_scores[i-1], (i, knn_scores[i-1]))
plt.xticks([i for i in range(1, 21)])
plt.xlabel('Number of Neighbors (K)')
plt.ylabel('Scores')
plt.title('K Neighbors Classifier scores for different K values')
Out[20]: Text(0.5, 1.0, 'K Neighbors Classifier scores for different K values')
```



As you can see, we achieved the maximum score of 87% when the number of neighbors was chosen to be 8.

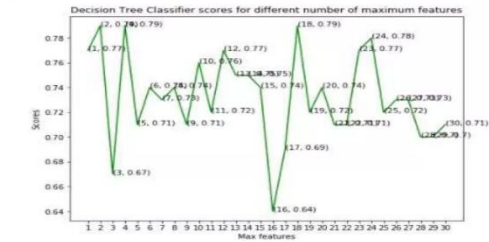
Decision Tree Classifier

This classifier creates a decision tree based on which, it assigns the class values to each data point. Here, we can vary the maximum number of features to be considered while creating the model. I range features from 1 to 30 (the total features in the dataset after dummy columns were added).

```
In [24]: dt_scores = []
for i in range(1, len(X.columns) + 1):
    dt_classifier = DecisionTreeClassifier(max_features = i, random_state = 0)
    dt_classifier.fit(X_train, y_train)
    dt_scores.append(dt_classifier.score(X_test, y_test))
```

Once we have the scores, we can then plot a line graph and see the effect of the number of features on the model scores.

```
In [25]: plt.plot([i for i in range(1, len(X.columns) + 1)], dt_scores, color = 'green')
for i in range(1, len(X.columns) + 1):
    plt.text(i, dt_scores[i-1], (i, dt_scores[i-1]))
plt.xticks([i for i in range(1, len(X.columns) + 1)])
plt.xlabel('Max Features')
plt.ylabel('Scores')
plt.title('Decision Tree Classifier scores for different number of maximum features')
Out[25]: Text(0.5, 1.0, 'Decision Tree Classifier scores for different number of maximum features')
```



From the line graph above, we can clearly see that the maximum score is 79% and is achieved for maximum features being selected to be either 2, 4 or 18.

Data Processing

To work with categorical variables, we should break each categorical column into dummy columns with 1s and 0s. Let's say we have a column Gender, with values 1 for Male and 0 for Female. It needs to be converted into two columns with the value 1 where the column would be true and 0 where it will be false. Take a look at the Gist below.

To get this done, we use the `get_dummies`

To get this done, we use the `get_dummies()` method from pandas. Next, we need to scale the dataset for which we will use the `StandardScaler`. The `fit_transform()` method of the scaler scales the data and we update the columns.

```
In [16]: df = pd.get_dummies(df, columns = ['sex', 'cp', 'fbs', 'restecg', 'exang', 'slope', 'ca', 'thal'])
standardScaler = StandardScaler()
columns_to_scale = ['age', 'trestbps', 'chol', 'thalach', 'oldpeak']
df[columns_to_scale] = standardScaler.fit_transform(df[columns_to_scale])
```

The dataset is now ready. We can begin with training our models.

Machine Learning In this project, I took 4 algorithms and varied their various parameters and compared the final models. I split the dataset into 67% training data and 33% testing data.

```
In [18]: y = df['target']
X = df.drop(['target'], axis = 1)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size = 0.33, random_state = 0)
```

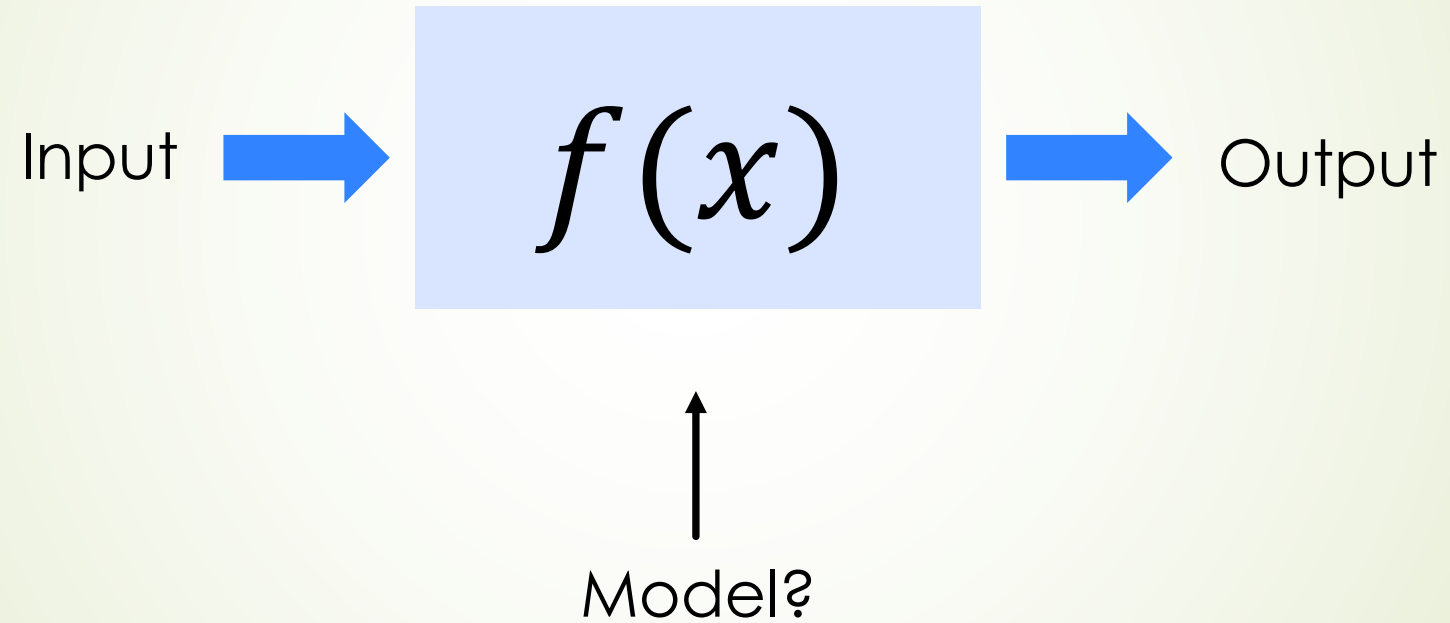
Conclusion

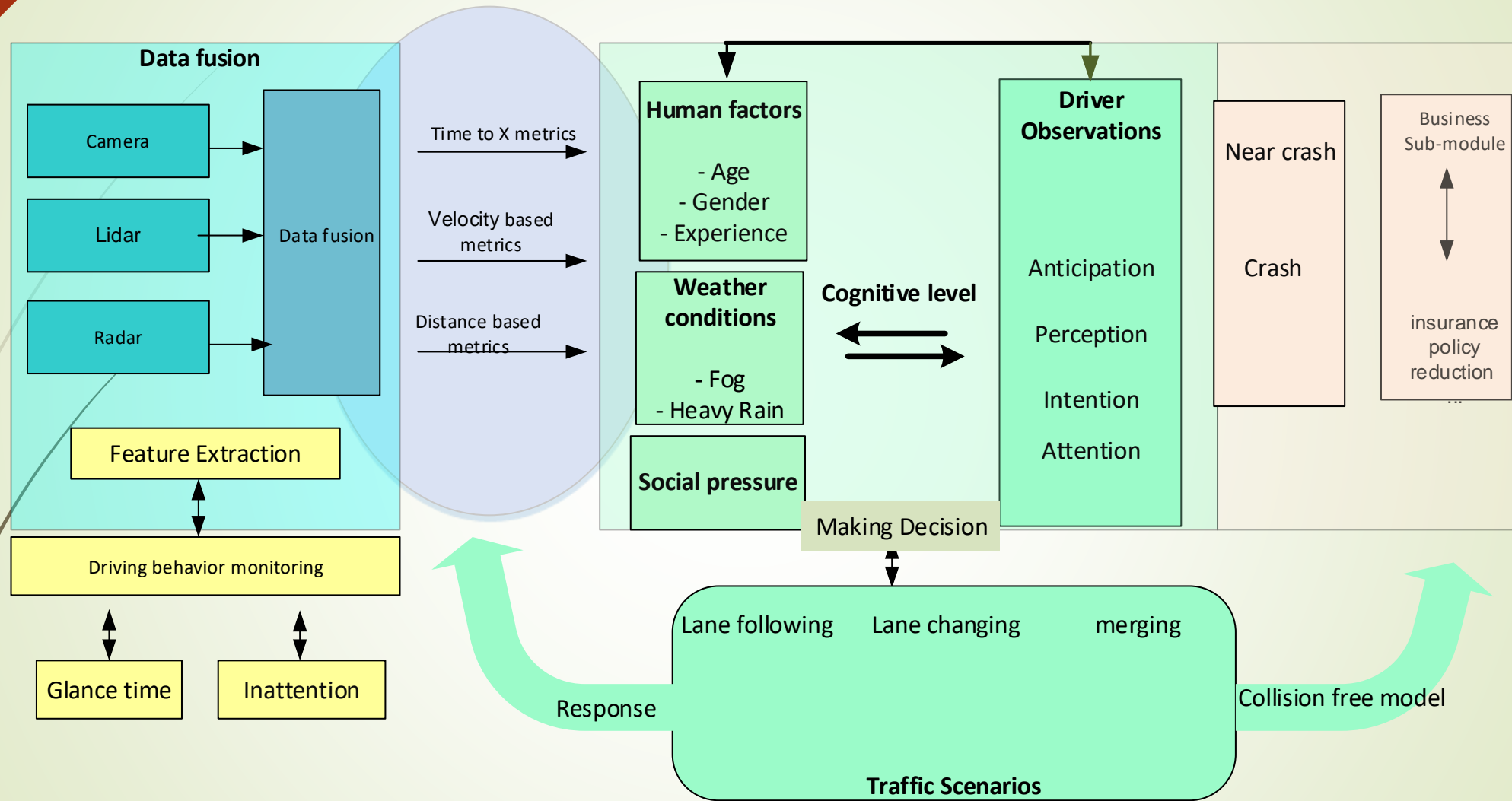
106

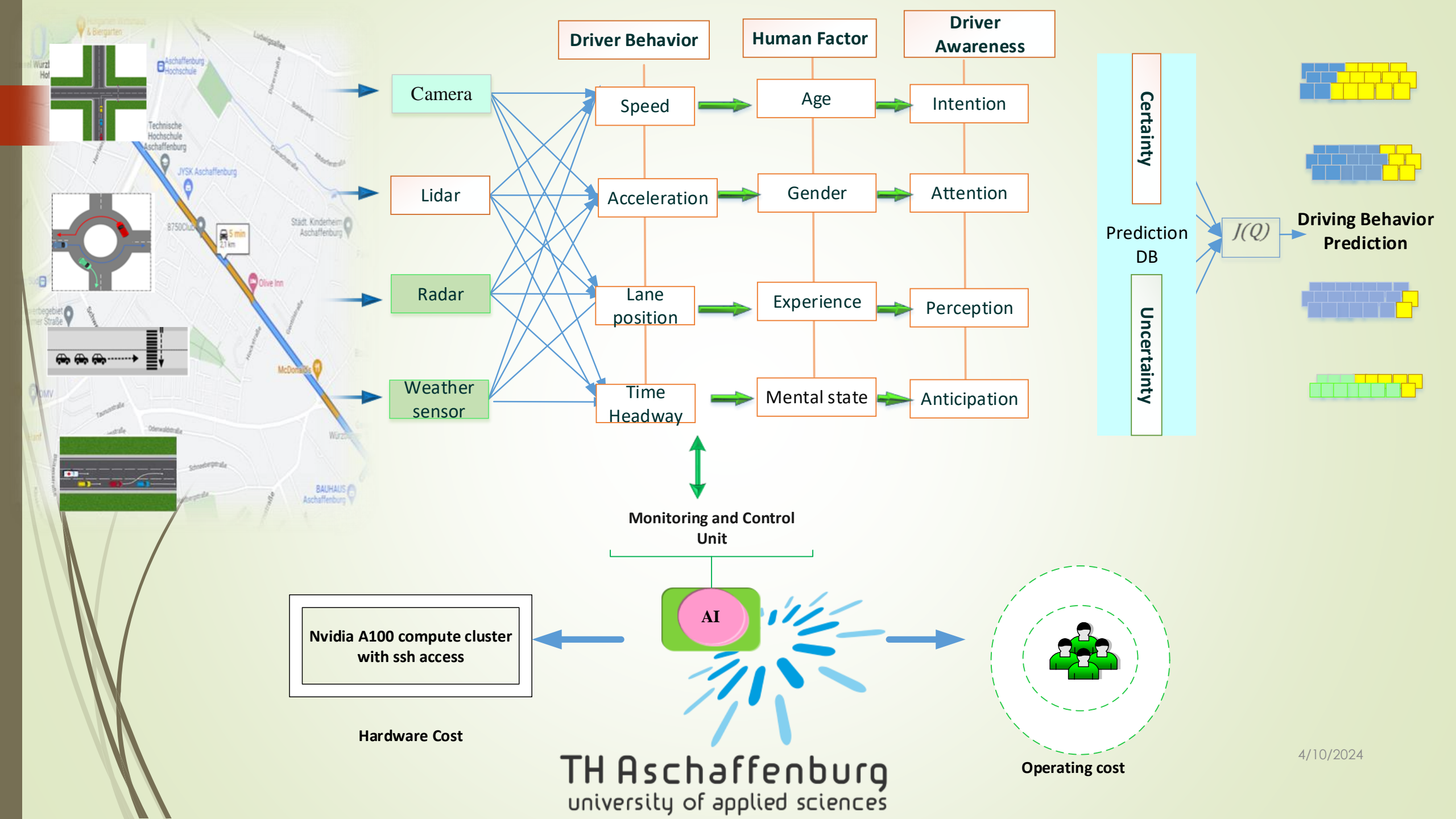
Introduction to Machine Learning

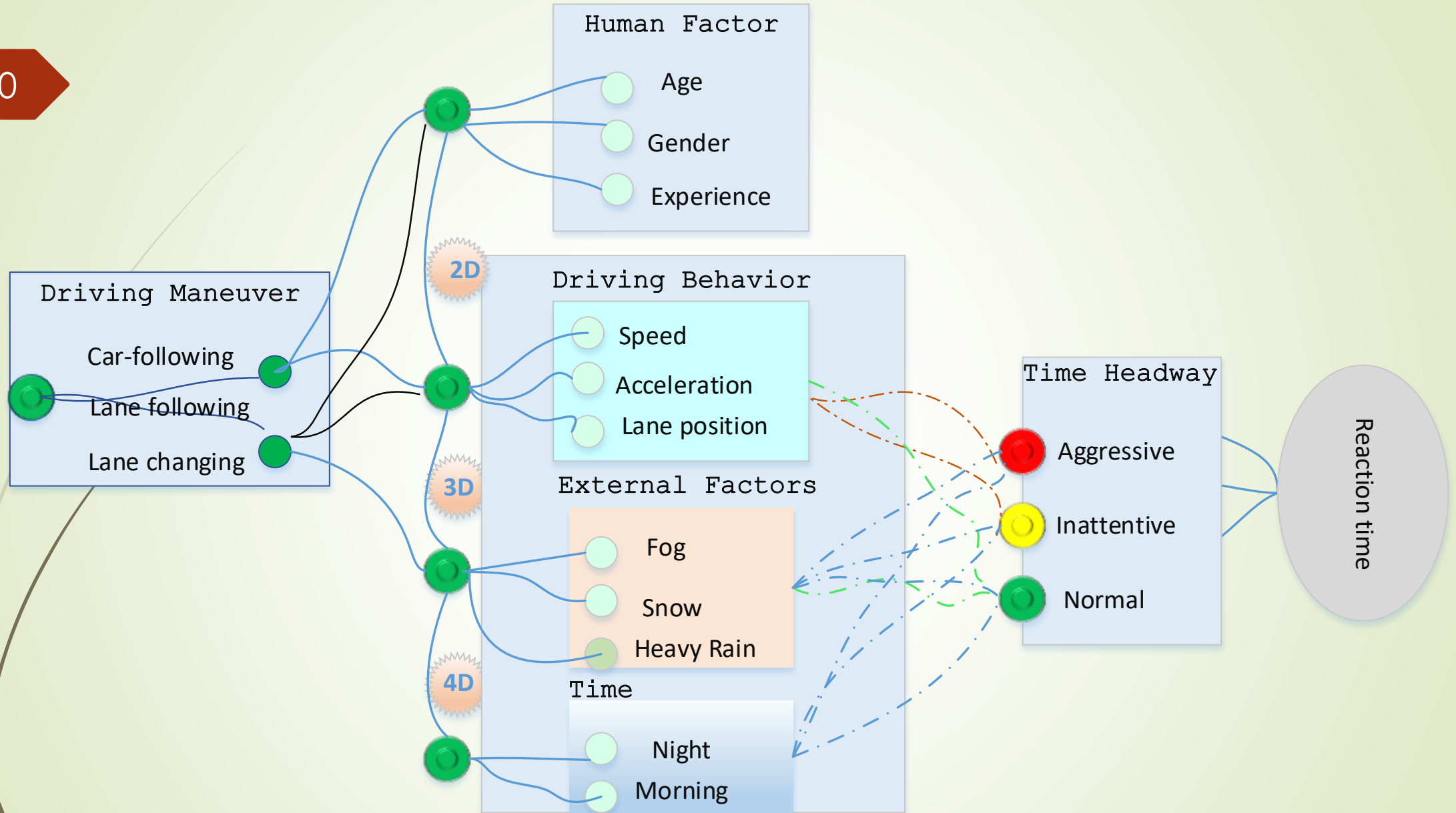
- Practical Examples
- General understanding of the model $f(x)$
- Deep Learning Approaches
 - Perceptron
 - Weights & biases can be trained
 - Activation function

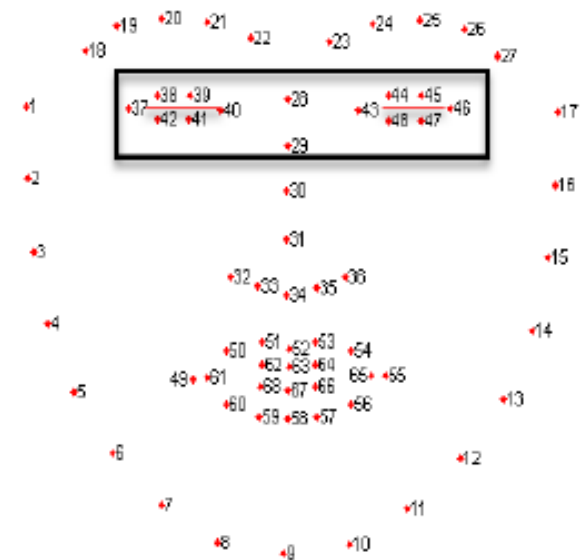
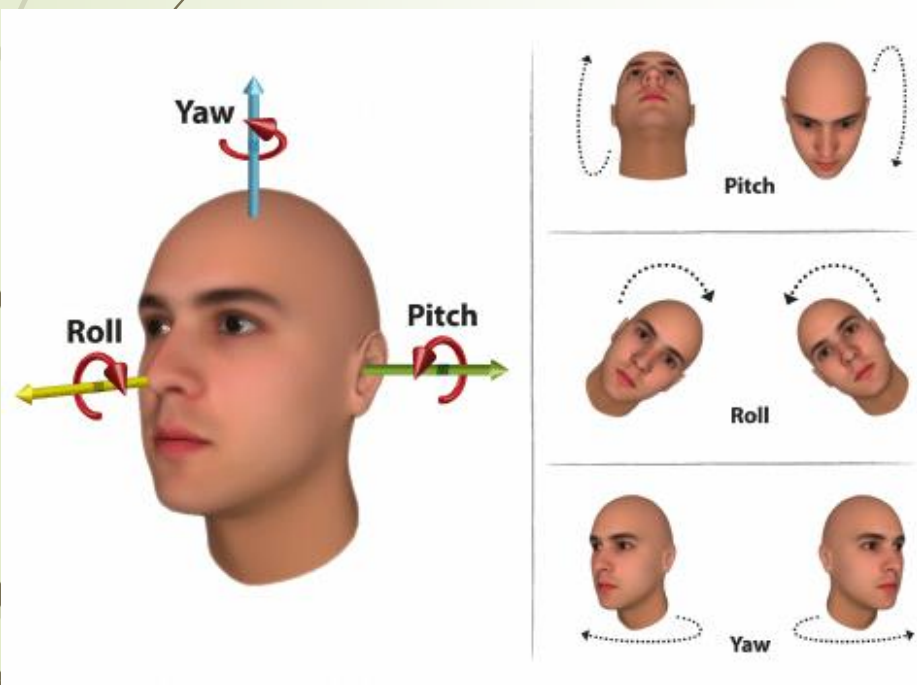
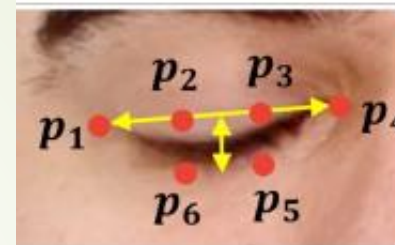
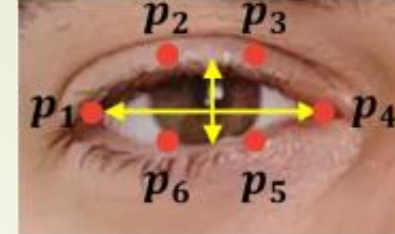
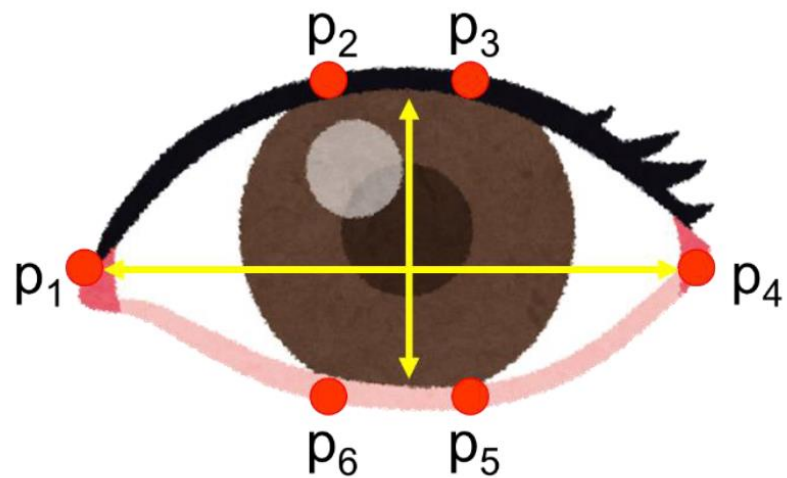
Driving Behavior











Thank You for Your Attention